## CHAPTER 6

## Teachers and Instruction

To provide information about mathematics teachers and instruction, Chapter 6 presents teachers' reports on their background and training and their instructional practices. Information also is presented about the materials used in instruction, the activities students do in class, the use of calculators and computers in mathematics lessons, the role of homework, and the reliance on different types of assessment approaches.


Teachers and the instructional approaches they use ultimately determine the mathematics students learn. Teachers structure the content and pace of lessons, introducing new material, selecting various instructional activities, and monitoring students' developing understanding of the mathematics concepts being studied. Teachers may help students use technology and tools to investigate mathematical ideas, analyze students' work for misconceptions, and promote positive attitudes toward mathematics. They may also assign homework and conduct informal as well as formal assessments to evaluate achievement outcomes.

To collect information about mathematics instruction, tIMss administered a two-part questionnaire in which teachers were asked to provide information about their background and training and their instructional practices. Information was also collected about the materials used in instruction, the activities students do in class, the use of calculators and computers in mathematics lessons, the role of homework, and the reliance on different types of assessment approaches. Chapter 6 presents teachers' responses to some of these questions.

Because the sampling for the teacher questionnaires was based on participating students, teachers' responses do not necessarily represent all eighth-grade mathematics teachers in each country. Rather, they represent teachers of the representative samples of students assessed. It is important to note that when information from the teacher questionnaire is being reported, the student is always the unit of analysis. That is, the data shown are the percentages of students whose teachers reported on various characteristics or instructional strategies. Using the student as the unit of analysis makes it possible to describe the instruction received by representative samples of students. Although this perspective may differ from that obtained by simply collecting information from teachers, it is consistent with the timss goals of providing information about the educational contexts and performance of students.

The teachers who completed the questionnaires were the mathematics teachers of the students who took the timss 1999 test. The general sampling procedure was to sample a mathematics class from each participating school, administer the test to those students, and ask their teacher to complete the questionnaire. Thus, the information about instruction is tied directly to the students tested. Sometimes, however, teachers did not complete the questionnaire assigned to them, so most
countries had some percentage of students for whom no teacher questionnaire information is available. The exhibits in this chapter have special notations on this point. For a country where teacher responses are available for 70 to 84 percent of the students, an " $r$ " is included next to its data. Where teacher responses are available for 50 to 69 percent of students, an "s" is included. Where teacher responses are available for less than $5^{\circ}$ percent, an "x" replaces the data.

## What Preparation Do Teachers Have for Teaching Mathematics?

This section presents information about background characteristics of mathematics teachers, including age and gender, major area of study, and certification. Teachers' confidence in teaching various mathematics topics is also discussed.

As shown in Exhibit 6.1, the majority of the eighth-grade students were taught mathematics by teachers in their $30 s$ and 40 . If there was a steady replenishing of the teaching force, one might expect approximately equivalent percentages of students taught by teachers in their 20s, 3os, 4 os, and 5 os. Very few countries, however, had a comparatively younger teaching force. Internationally on average, only 16 percent of students were taught by teachers younger than age 30 . The three countries with the most students (about one-third) taught by younger teachers were Hong Kong, Iran, and Singapore. Although 21 percent of the students internationally were taught by teachers age $5^{\circ}$ or older, the teaching force was relatively older in a number of countries. About one-third or more of the students (from 32 to 47 percent) in Chile, the Czech Republic, Finland, Italy, Macedonia, Moldova, Romania, and the Slovak Republic had teachers at least 50 years of age.

Internationally on average, 6o percent of eighth-grade students were taught mathematics by females and 40 percent by males, and similar percentages were found in a number of countries. However, at least 75 percent of students had female teachers in Bulgaria, Hungary, Israel, Italy, Latvia (Lss), Lithuania, Moldova, the Philippines, the Russian Federation, Singapore, the Slovak Republic, and Slovenia. By contrast, in no country were as many as three-fourths of the students taught mathematics by male teachers. The three countries with the most students taught by male teachers were Iran (7o percent), Japan (73 percent), and the Netherlands ( 72 percent).

Exhibit 6.2 presents teachers' reports about their major areas of study and certification. Teachers' undergraduate and graduate studies provide some indication of their preparation to teach mathematics. On average internationally, 84 percent of students were taught by teachers having mathematics and/or mathematics education as a major area of study. Teachers can have dual majors, or different majors at the undergraduate and graduate level. Exhibit R3. 1 in the reference section provides detail for each of the following major areas of study: mathematics,
 mathematics education, science or science education, education (other than mathematics or science education), and other, which includes majors in any other areas.

|  | Percentage of Students by Age of Teachers |  |  |  | Percentage of Students by Gender of Teachers |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 29 Years or Under | 30-39 Years | 40-49 Years | 50 Years or Older | Female | Male |
| Australia Belgium (Flemish) Bulgaria Canada Chile | $\begin{array}{r} 23(4.0) \\ 20(2.7) \\ 8(2.4) \\ 17(2.4) \\ 3(1.1) \end{array}$ | $\begin{array}{ll} 25 & (3.3) \\ 15 & (2.4) \\ 33 & (5.7) \\ 33 & (2.7) \\ 17 & (2.7) \end{array}$ | 36 (4.1) <br> 38 (3.0) <br> 38 (4.8) <br> 25 (3.1) <br> 47 (3.6) | $\begin{array}{ll} 16 & (3.0) \\ 27 & (3.1) \\ 21 & (4.1) \\ 26 & (3.0) \\ 33 & (3.5) \end{array}$ | 42 (4.3) <br> 66 (4.8) <br> 87 (2.8) <br> 53 (3.0) <br> 45 (3.9) | 58 (4.3) <br> 34 (4.8) <br> 13 (2.8) <br> 47 (3.0) <br> 55 (3.9) |
| Chinese Taipei Cyprus Czech Republic England Finland | $\begin{array}{rr}  & 10(2.6) \\ & 3(1.0) \\ & 7(2.5) \\ 5 & 20(2.9) \\ & 10(2.8) \end{array}$ | 34 (4.0) <br> 42 (4.1) <br> 29 (4.8) <br> 23 (3.5) <br> 15 (2.8) | 30 (4.0) <br> 33 (3.5) <br> 22 (5.0) <br> 35 (3.6) <br> 30 (3.6) | $\begin{aligned} & 26(3.4) \\ & 23(3.4) \\ & 43(5.6) \\ & 22(2.7) \\ & 45(4.4) \end{aligned}$ | $51(4.1)$ $67(4.4)$ $73(4.0)$ $48(3.8)$ $59(4.4)$ | 49 (4.1) <br> 33 (4.4) <br> 27 (4.0) <br> 52 (3.8) <br> 41 (4.4) |
| Hong Kong, SAR <br> Hungary <br> Indonesia <br> Iran, Islamic Rep. Israel | $\begin{array}{r} 32(4.2) \\ 8(2.3) \\ 23(3.8) \\ 36(4.8) \\ 21(3.0) \end{array}$ | $\begin{array}{ll} 38 & (4.5) \\ 20 & (3.2) \\ 50 & (3.9) \\ 23 & (3.1) \\ 26 & (3.2) \end{array}$ | $\begin{array}{ll} 19 & (3.3) \\ 46 & (4.1) \\ 20 & (3.3) \\ 39 & (4.8) \\ 36 & (3.4) \end{array}$ | $\begin{array}{r} 11(2.6) \\ 26(3.2) \\ 8(2.6) \\ 2(1.2) \\ 17(2.5) \end{array}$ | $\begin{array}{ll} 44 & (4.1) \\ 80 & (3.2) \\ 44 & (4.7) \\ 30 & (3.8) \\ 78 & (3.1) \end{array}$ | $\begin{array}{ll} 56 & (4.1) \\ 20 & (3.2) \\ 56 & (4.7) \\ 70 & (3.8) \\ 22 & (3.1) \end{array}$ |
| Italy Japan Jordan Korea, Rep. of Latvia (LSS) | $\begin{array}{r} 0(0.0) \\ 21(3.3) \\ 27(3.7) \\ 19(3.0) \\ 14(3.2) \end{array}$ | $\begin{array}{r} 8(2.0) \\ 39(4.3) \\ 45(4.6) \\ 53(3.7) \\ 33 \end{array}$ | 58 (4.1) <br> 33 (3.7) <br> 24 (3.2) <br> 15 (2.5) <br> 28 (4.4) | $\begin{array}{r} 34(3.8) \\ 7(2.1) \\ 4(1.5) \\ 13(2.8) \\ 25(4.2) \end{array}$ | 76 (3.1) <br> 27 (3.6) <br> 48 (4.5) <br> 59 (3.4) <br> 91 (2.6) | $\begin{array}{r} 24(3.1) \\ 73(3.6) \\ 52(4.5) \\ 41(3.4) \\ 9(2.6) \end{array}$ |
| Lithuania ${ }^{\ddagger}$ Macedonia, Rep. of Malaysia <br> Moldova <br> Morocco | $\begin{array}{r} 5(1.7) \\ 1(0.9) \\ 28(3.6) \\ 4(1.7) \\ 4(1.3) \end{array}$ | $\begin{aligned} & 34(4.1) \\ & 29(3.6) \\ & 39(4.4) \\ & 24(4.0) \\ & 34(3.2) \end{aligned}$ | $\begin{aligned} & 32(3.9) \\ & 23(3.6) \\ & 27(3.6) \\ & 39(4.0) \\ & 58(3.2) \end{aligned}$ | $\begin{array}{r} 29(4.0) \\ 47(3.5) \\ 6(1.8) \\ 33(4.3) \\ 4(1.0) \end{array}$ | $\begin{array}{ll} 90 & (2.5) \\ 50 & (4.6) \\ 68 & (3.6) \\ 76 & (3.6) \\ 39 & (3.1) \end{array}$ | $\begin{array}{ll} 10 & (2.5) \\ 50 & (4.6) \\ 32 & (3.6) \\ 24 & (3.6) \\ 61 & (3.1) \end{array}$ |
| Netherlands <br> New Zealand Philippines Romania Russian Federation | $\begin{array}{r} 15(4.3) \\ 16(3.3) \\ 25(3.6) \\ 8(2.1) \\ 8(2.0) \end{array}$ | $\begin{aligned} & 17(3.9) \\ & 19(3.4) \\ & 37(4.1) \\ & 19(3.6) \\ & 32(3.7) \end{aligned}$ | 41 (5.4) <br> 35 (4.2) <br> 23 (3.2) <br> 30 (4.2) <br> 29 (2.9) | $\begin{aligned} & 26(5.3) \\ & 30(4.2) \\ & 15(2.7) \\ & 42(4.2) \\ & 31 \end{aligned}(4.0)$ | $\begin{array}{ll} 28 & (5.0) \\ 44 & (4.0) \\ 75 & (3.9) \\ 63 & (4.1) \\ 93 & (2.6) \end{array}$ | $\begin{array}{r} 72(5.0) \\ 56(4.0) \\ 25(3.9) \\ 37(4.1) \\ 7(2.6) \end{array}$ |
| Singapore Slovak Republic Slovenia South Africa Thailand | $\begin{array}{r} 37(4.4) \\ 9(2.4) \\ 6(1.6) \\ 29(3.4) \\ 23(3.2) \end{array}$ | $\begin{array}{ll} 25 & (4.0) \\ 21 & (3.9) \\ 43 & (4.3) \\ 55 & (4.1) \\ 28 & (3.6) \end{array}$ | 15 (3.2) <br> 38 (4.8) <br> 39 (4.2) <br> 13 (3.2) <br> 43 (3.7) | $\begin{array}{r} 23(3.6) \\ 32(4.3) \\ 12(2.7) \\ 3(1.3) \\ 6(2.1) \end{array}$ | $\begin{array}{ll} 75 & (4.1) \\ 86 & (3.3) \\ 89 & (2.8) \\ 39 & (4.9) \\ 69 & (3.7) \end{array}$ | $\begin{array}{ll} 25 & (4.1) \\ 14 & (3.3) \\ 11 & (2.8) \\ 61 & (4.9) \\ 31 & (3.7) \end{array}$ |
| Tunisia <br> Turkey <br> United States | $\begin{array}{ll} 21 & (3.0) \\ 23 & (3.4) \\ 11 & (2.0) \end{array}$ | $\begin{aligned} & 35(3.9) \\ & 15 \\ & 25 \\ & 25 \end{aligned}$ | $\begin{array}{ll} 40 & (4.2) \\ 56 & (3.9) \\ 37 & (3.9) \end{array}$ | $\begin{array}{r} 4(1.7) \\ 5(2.3) \\ 27(2.9) \end{array}$ | $\begin{array}{ll} 39 & (4.3) \\ 41 & (3.9) \\ 60 & (3.0) \end{array}$ | $\begin{array}{ll} 61 & (4.3) \\ 59 & (3.9) \\ 40 & (3.0) \end{array}$ |
| International Avg. | 16 (0.5) | 30 (0.6) | 33 (0.6) | 21 (0.5) | 60 (0.6) | 40 (0.6) |

[^0][^1]

[^2]$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning at the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
A dash ( - ) indicates data are not available.
An " $r$ " indicates teacher response data available for $70-84 \%$ of students. An " $s$ " indicates teacher response data available for $50-69 \%$ of students.

Eighty-five percent of students, on average internationally, were taught mathematics by teachers having a teaching certificate in any subject. In TIMSS 1995, detailed information collected about certification indicated a wide range of criteria across countries. ${ }^{1}$ For example, the number of years of post-secondary education required for a teaching qualification ranged from two years in Iran to as many as six years in Canada; many countries reported four years. Almost all countries reported that teaching practice was required, and a large number reported that an evaluation or examination was required for certification. In some countries, such as the United States, the types of certification varied according to the policies of different states. Despite difficulties in interpretation illustrated by the 1995 data, however, it is interesting to note that in timss 1999 the percentages of students taught by teachers reporting that they had a certificate ranged from 32 percent in Cyprus to 100 percent in Australia, Hungary, Japan, and Singapore. There was even more variation among countries when both certification and having had mathematics as a major were considered. The percentage of students taught by teachers both certified and having had mathematics or mathematics education as a major ranged from 25 percent in Canada to 99 percent in Hungary and Macedonia, with an international average of 73 percent.

To gauge teachers' confidence to teach mathematics topics, timss constructed an index of teachers' confidence in their preparation to teach mathematics (CPTM), presented in Exhibit 6.3. Teachers were asked how well prepared they felt to teach each of 12 mathematics topics (e.g., properties of geometric figures, solving linear equations and inequalities). Responses were given on a three-point scale; very well prepared was assigned a value of three, somewhat prepared two, and not well prepared one. Students were assigned to the high level of the index if their teachers reported that they felt very well prepared, on average across the 12 topics ( 2.75 or higher). The medium level indicates that teachers reported being somewhat to well prepared (averages from 2.25 to 2.75 ), and the low level that they reported being only somewhat prepared or less (averages less than 2.25).

The results show that average mathematics achievement is related to how well teachers felt they were prepared to teach mathematics, with higher achievement related to higher levels of teachers' confidence in their preparation. On average internationally, teachers reported relatively high degrees of confidence, with 63 percent of students taught by teachers who believed they were very well prepared. Countries where 85 percent or more of the students were taught by teachers who believed they were very well prepared were Macedonia, the United States, the Slovak Republic,

[^3]Cyprus, Jordan, New Zealand, and the Czech Republic. Interestingly, countries with substantial percentages of students whose teachers reported a low level of confidence included both high- and low-performing countries. One-third or more of the students in Chile, Hungary, Japan, Slovenia, Thailand, and Tunisia were taught by teachers feeling only somewhat prepared or less.

The detail for the 12 topics included in the index is provided in Exhibit R3.2 in the reference section. On average across countries, the topics having the most students (from 79 to 82 percent) taught by teachers who felt very well prepared were fractions, decimals, and percentages; ratios and proportions; perimeter, area, and volume; evaluate and perform operations on algebraic expressions; and solving linear equations and inequalities. Teachers reported being least well prepared to teach understanding and calculations related to simple probabilities; just more than half the students internationally ( 55 percent on average) were taught by teachers who felt very well prepared to teach this topic. Exhibit R3.3 shows principals' opinions about the degree to which shortages of qualified mathematics teachers affect the capacity to provide instruction. On average internationally, principals reported that such shortages affect the quality of instruction some or a lot for one-third of the students. Bulgaria, Jordan, Moldova, Tunisia, and Turkey reported shortages affecting capacity to provide instruction a lot for more than half their students.

Teachers' beliefs about mathematics learning and instruction are to some degree related to their preparation. Exhibits R3.4 and R3.5 in the reference section show the percentages of eighth-grade students whose mathematics teachers reported certain beliefs about mathematics, the way mathematics should be taught, and the importance of various cognitive skills in achieving success in the discipline. In general, there was substantial agreement about the inherent nature of mathematical abilities. For example, in most countries 8o percent or more of students had teachers who agreed that some students have a natural talent for mathematics. There was also nearly complete agreement that more than one representation should be used in teaching a mathematics topic. The greatest variation in views pertained to the importance of being able to remember formulas and procedures; only about 10 percent of students in Slovenia were taught by teachers who believed this ability was very important for students' success in mathematics, while about 90 percent of students in the Philippines had teachers who believed that to be the case.

## Index of Teachers' Confidence in Preparation to Teach Mathematics

Index based on teachers' responses to 12 questions about how prepared they feel to teach different mathematics topics (see reference exhibit R3.2) based on a 3-point scale: $1=$ not well prepared; 2 = somewhat prepared; 3 = very well prepared. Average is computed across the 12 items for items for which the teacher did not respond do not teach. High level indicates average is greater than or equal to 2.75. Medium level indicates average is greater than or equal to 2.25 and less than 2.75. Low level indicates average is less than 2.25.

| Macedonia, Rep. of United States | High CPTM |  | Medium CPTM |  | Low <br> CPTM |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
|  | 92 (2.2) | 447 (4.7) | 8 (2.1) | 435 (16.2) | 1 (0.6) | ~ ~ |
|  | 87 (2.4) | 505 (4.2) | 11 (2.3) | 489 (7.0) | 2 (1.0) | ~ ~ |
| Slovak Republic | 87 (3.2) | 532 (3.8) | 11 (3.1) | 531 (14.1) | 2 (1.3) | ~ |
| Cyprus | 87 (2.7) | 478 (1.8) | 13 (2.7) | 468 (6.6) | 0 (0.0) | ~ |
| Jordan | 86 (3.0) | 429 (3.8) | 11 (2.7) | 418 (11.0) | 3 (1.3) | 400 (15.9) |
| New Zealand | 85 (3.0) | 496 (5.4) | 10 (2.5) | 460 (15.7) | 5 (1.7) | 459 (19.2) |
| Czech Republic | 85 (3.6) | 521 (5.1) | 14 (3.8) | 519 (9.5) | 1 (1.3) | ~ ~ |
| Netherlands | 81 (6.2) | 542 (7.1) | 10 (3.0) | 514 (22.4) | $9(5.8)$ | 514 (58.7) |
| Romania | 79 (3.5) | 478 (6.6) | 20 (3.5) | 453 (8.8) | 1 (0.0) | ~ |
| Australia | 77 (4.1) | 529 (5.7) | 16 (3.4) | 521 (9.8) | 6 (2.3) | 502 (23.9) |
| Finland | 76 (3.0) | 522 (3.2) | 15 (3.0) | 523 (7.0) | 10 (1.9) | 507 (7.8) |
| Malaysia | 75 (3.9) | 525 (5.1) | 20 (3.3) | 511 (10.3) | 5 (2.3) | 462 (28.2) |
| Israel | 75 (2.8) | 472 (5.5) | 21 (2.4) | 464 (7.7) | 5 (1.8) | 448 (15.0) |
| Turkey | 75 (3.1) | 434 (5.5) | 21 (2.9) | 412 (7.6) | 4 (1.4) | 406 (9.1) |
| Iran, Islamic Rep. | 72 (3.6) | 425 (4.2) | 25 (3.5) | 420 (6.8) | 3 (1.4) | 388 (8.8) |
| Chinese Taipei | 71 (3.6) | 586 (4.5) | 15 (3.1) | 587 (10.9) | 14 (2.7) | 572 (6.8) |
| Canada | 71 (2.7) | 537 (3.3) | 21 (3.0) | 530 (6.6) | 8 (1.8) | 515 (14.6) |
| Indonesia | 69 (4.7) | 411 (5.9) | 27 (4.5) | 377 (8.8) | 4 (1.7) | 447 (21.5) |
| Singapore | 66 (4.2) | 603 (7.1) | 24 (3.7) | 619 (12.0) | 10 (2.8) | 578 (20.8) |
| Belgium (Flemish) | 65 (3.2) | 559 (5.8) | 32 (3.1) | 561 (5.6) | 3 (1.4) | 558 (27.1) |
| Latvia (LSS) | 64 (4.3) | 508 (4.8) | 28 (4.4) | 504 (6.8) | 8 (2.3) | 489 (11.1) |
| Hong Kong, SAR | 61 (4.3) | 579 (5.5) | 28 (3.9) | 591 (8.2) | 11 (2.7) | 571 (12.0) |
| Italy | 60 (3.9) | 479 (5.5) | 27 (3.5) | 481 (7.2) | 13 (2.3) | 479 (12.4) |
| Morocco | 57 (2.9) | 336 (3.7) | 37 (2.8) | 338 (4.4) | 7 (1.3) | 340 (8.7) |
| Bulgaria | 54 (5.4) | 517 (9.7) | 29 (4.6) | 515 (9.4) | 17 (5.8) | 488 (10.0) |
| Hungary | 54 (4.1) | 531 (5.2) | 12 (2.8) | 526 (12.1) | 34 (3.7) | 533 (6.6) |
| South Africa | 54 (4.0) | 290 (10.5) | 33 (3.6) | 256 (9.2) | 14 (2.7) | 266 (14.2) |
| Moldova | 52 (4.5) | 465 (5.1) | 27 (3.8) | 473 (8.1) | 21 (3.6) | 471 (11.4) |
| Korea, Rep. of | 48 (3.9) | 585 (3.2) | 31 (3.8) | 590 (4.1) | 21 (3.0) | 588 (3.5) |
| Philippines | 41 (3.8) | 355 (8.8) | 44 (3.9) | 341 (8.7) | 14 (2.9) | 326 (13.1) |
| Slovenia | 34 (3.5) | 530 (4.3) | 32 (3.7) | 530 (4.9) | 34 (4.0) | 530 (5.0) |
| Tunisia | 25 (3.7) | 447 (4.7) | 42 (4.1) | 447 (3.5) | 34 (3.7) | 449 (4.8) |
| Chile | 24 (3.2) | 405 (9.1) | 31 (3.2) | 385 (5.5) | 45 (3.7) | 391 (7.5) |
| Thailand | 18 (3.5) | 487 (15.6) | 26 (3.8) | 468 (10.6) | 55 (4.4) | 461 (6.1) |
| Japan | 8 (2.1) | 584 (6.1) | 24 (3.6) | 589 (4.2) | 68 (4.0) | 573 (2.6) |
| England | -- | -- | -- | -- | -- | -- |
| Lithuania * | -- | -- | -- | -- | -- | -- |
| Russian Federation | -- | -- | -- | -- | -- | -- |
| International Avg. | 63 (0.6) | 489 (1.1) | 23 (0.6) | 481 (1.7) | 14 (0.5) | 473 (2.9) |

[^4]

## How Much School Time Is Devoted to Mathematics Instruction?

Exhibit 6.4 presents information about the amount of mathematics instruction given to eighth-grade students in the timss 1999 countries. Since different systems have school years of different lengths (see reference Exhibit R3.6) and different arrangements of weekly and daily instruction, the comparisons are given in terms of the average number of hours of mathematics instruction over the school year as reported by mathematics teachers. Countries providing 150 or more hours per year were Indonesia, Morocco, Thailand, Chile, and Canada. Countries providing fewer than 100 hours were Bulgaria, Turkey, the Netherlands, Finland, Macedonia, and Cyprus. The percentage of instructional time at the eighth grade that was devoted to mathematics ranged from 17 percent in Indonesia and the Russian Federation to nine percent in Chinese Taipei, Cyprus, and the Netherlands (see Exhibit R3.7 for details on the total instructional time in each country). For most countries, the percentages of time devoted to mathematics reported by teachers correspond with the percentages targeted in the intended curriculum (see Exhibit $5 \cdot 5$ ).

As shown in Exhibit 6.5, teachers of about half the students, on average internationally, reported that mathematics classes meet for at least two hours per week but fewer than three and a half. For another one-third of students, classes meet for at least three and a half hours but fewer than five. At least three and a half hours per week of mathematics instruction was reported for more than 50 percent of the students in Canada, Chile, the Czech Republic, Hong Kong, Indonesia, Israel, Italy, Latvia (Lss), Moldova, Morocco, New Zealand, the Russian Federation, the Slovak Republic, South Africa, Tunisia, and the United States. The data reveal no clear pattern between the number of in-class instructional hours and mathematics achievement either across or within countries. Common sense and research both support the idea that time on task is an important contributor to achievement, yet this time can be spent more or less efficiently. Time alone is not enough; it needs to be spent on high-quality mathematics instruction. Devoting extensive class time to remedial activities can deprive students of this. Also, instructional time can be spent out of school in various tutoring programs; low-performing students may be receiving additional instruction.

Exhibit 6.6 shows trends between 1995 and 1999 in the number of hours mathematics is taught weekly. On average internationally, the students receiving at least two hours of mathematics instruction per week but fewer than three and a half increased significantly by five percentage points, and those receiving three and a half to fewer than five hours decreased by seven percentage points. There was little change internationally in the percentage of students receiving five hours or more. The Czech Republic and the Slovak Republic showed a decrease in the weekly hours of mathematics instruction. Belgium (Flemish) and Singapore showed a significant increase in the percentage of students receiving five hours or more of instruction per week.

Videotapes of mathematics classes in the United States and Japan in TImSS 1995 revealed that outside interruptions can affect the flow of the lesson and detract from instructional time. ${ }^{2}$ As shown in Exhibit 6.7, on average internationally about one-fifth of the students ( 21 percent) tested in timss 1999 were in mathematics classes that were interrupted pretty often or almost always. In comparison, 28 percent were in classes that were never interrupted; in Japan, Korea, and Tunisia, more than half the students were in such classes.

Across countries, students' mathematics teachers spent only about 60 percent of their formally scheduled school time teaching mathematics (see Exhibit R3. 8 in the reference section). Of the remaining time, about 10 percent was spent teaching subjects other than mathematics,
$\Gamma^{6}$
 about 10 percent on curriculum planning, and about 20 percent on a various administrative and other duties.

[^5]

[^6][^7]
$\square$


|  | 5 Hours or More |  | 3.5 Hours to < 5 |  | 2 Hours to < 3.5 |  | Less Than 2 Hours |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Australia Belgium (Flemish) Bulgaria Canada Chile | $\begin{array}{r} 3(1.7) \\ 4(1.0) \\ 4(3.0) \\ 17(2.2) \\ 13(2.4) \end{array}$ | $\begin{aligned} & 530(46.0) \\ & 590 \text { (11.7) } \\ & 606 \text { (29.5) } \\ & 520 \text { (6.4) } \\ & 394 \text { (13.7) } \end{aligned}$ | $\begin{array}{r} 44(4.4) \\ 40(2.8) \\ 8(2.3) \\ 55(3.2) \\ 83 \end{array}$ | $\begin{aligned} & 534(7.7) \\ & 595(4.1) \\ & 525(27.0) \\ & 544(3.9) \\ & 391(5.0) \end{aligned}$ | $\begin{array}{r} 50(4.6) \\ 43(3.8) \\ 73(4.6) \\ 26(2.7) \\ 3(1.3) \end{array}$ | $\begin{aligned} & 517(6.7) \\ & 544(7.7) \\ & 498(5.0) \\ & 523(6.1) \\ & 414(12.7) \end{aligned}$ | $\begin{array}{r} 3(1.4) \\ 13(3.4) \\ 14(3.3) \\ 3(0.9) \\ 1(0.7) \end{array}$ | $\begin{gathered} 565(30.5) \\ 502(18.9) \\ 543(9.0) \\ 503(6.3) \\ \sim \sim \end{gathered}$ |
| Chinese Taipei Cyprus Czech Republic England Finland | $\begin{array}{ll} 1 & (1.1) \\ 0 & (0.0) \\ 4 & (2.1) \\ 2 & (1.2) \\ 1 & (0.9) \end{array}$ | $600 \text { (28.1) }$ | $\begin{array}{r} 48(4.4) \\ 0(0.0) \\ 52(4.4) \\ 3(1.4) \\ 7(2.4) \end{array}$ | $\begin{gathered} 592(5.8) \\ \sim \sim \\ \sim 17(5.3) \\ 481(10.2) \\ 535(14.0) \end{gathered}$ | $\begin{array}{r} 51(4.5) \\ 100(0.0) \\ 44(4.4) \\ 95(2.0) \\ 87(2.9) \end{array}$ | 577 (5.5) 476 (1.8) 517 (6.4) 512 (5.3) 520 (2.9) | $\begin{array}{ll} 0 & (0.0) \\ 0 & (0.0) \\ 0 & (0.0) \\ 0 & (0.2) \\ 4 & (1.5) \end{array}$ | $518 \text { (12.2) }$ |
| Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel | $\begin{array}{r} 9(2.3) \\ 3(1.1) \\ 21(3.7) \\ 12(2.6) \\ 4(1.5) \end{array}$ | $\begin{array}{ll} 579 & (15.2) \\ 583 & \text { (34.4) } \\ 384 \text { (9.4) } \\ 419 & (11.4) \\ 470 & (28.7) \end{array}$ | $\begin{array}{ll} 71(4.0) \\ 15 & (2.7) \\ 76 & (3.8) \\ 14(2.9) \\ 65 & (4.1) \end{array}$ | $\begin{aligned} & 583 \text { (5.6) } \\ & 522 \text { (12.6) } \\ & 408 \text { (6.1) } \\ & 413(8.9) \\ & 464(5.8) \end{aligned}$ | $\begin{array}{r} 17(3.1) \\ 80(2.9) \\ 1(0.2) \\ 50(4.8) \\ 29(3.9) \end{array}$ | $\begin{gathered} 587(11.1) \\ 531(3.9) \\ \sim \sim \\ 423(4.9) \\ 481(8.5) \end{gathered}$ | $\begin{array}{r} 3(1.5) \\ 1(0.8) \\ 3(1.2) \\ 24(4.0) \\ 2(1.2) \end{array}$ | $\begin{gathered} 553(16.7) \\ \sim \sim \\ 409(27.4) \\ 429(5.7) \\ \sim \sim \end{gathered}$ |
| Italy Japan Jordan Korea, Rep. of Latvia (LSS) | $\begin{array}{ll} 9 & (2.1) \\ 1 & (1.3) \\ 5 & (1.9) \\ 2(0.9) \\ 7 & (2.5) \end{array}$ | $\begin{gathered} 469(11.5) \\ \sim \sim \\ 463(21.0) \\ \sim \sim \\ \sim 87 \\ \sim \end{gathered}$ | $\begin{array}{r} 55(3.8) \\ 2(1.3) \\ 7(2.2) \\ 3(1.1) \\ 62(3.9) \end{array}$ | $\begin{gathered} 483(5.3) \\ \sim \\ \sim \\ 439(20.1) \\ 602(9.6) \\ 516(4.6) \end{gathered}$ | 29 (4.0) <br> 95 (2.0) <br> 88 (2.8) <br> 93 (1.8) <br> 31 (4.2) | $\begin{aligned} & 475(7.4) \\ & 577(2.1) \\ & 424(3.7) \\ & 587(2.1) \\ & 491(5.6) \end{aligned}$ | $\begin{aligned} & 6(1.8) \\ & 2(0.9) \\ & 0(0.0) \\ & 3(1.1) \\ & 0(0.0) \end{aligned}$ | $\begin{aligned} & 484(10.3) \\ & \sim \sim \\ & \sim \sim \\ & 587(11.7) \\ & \sim \sim \end{aligned}$ |
| Lithuania $\ddagger$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | $\begin{aligned} & -- \\ & 0(0.0) \\ & 0(0.0) \\ & 8(2.4) \\ & 96(1.1) \end{aligned}$ | $\begin{aligned} & 481 \text { (17.9) } \\ & 337(2.9) \end{aligned}$ | $\begin{array}{r} -- \\ 2(1.0) \\ 2(1.2) \\ 80(3.3) \\ 0(0.0) \end{array}$ | $466 \text { (4.5) }$ | $\begin{array}{r} 97(1.2) \\ 93(2.1) \\ 5(1.5) \\ 3(1.0) \end{array}$ | $\quad--$ $447(4.4)$ $520(4.6)$ $485(18.0)$ $338(10.5)$ | $\begin{array}{ll} 1 & (0.6) \\ 5 & (1.8) \\ 7 & (1.9) \\ 1 & (0.6) \end{array}$ | $\begin{gathered} 533 \text { (24.0) } \\ 467 \text { (19.7) } \\ \sim \sim \end{gathered}$ |
| Netherlands <br> New Zealand <br> Philippines <br> Romania <br> Russian Federation | $\begin{array}{r} 0(0.0) \\ 1(0.0) \\ 11(2.5) \\ 9(2.5) \\ 11(2.5) \end{array}$ | $326 \text { (15.0) }$ <br> 477 (21.8) <br> 553 (13.4) | $\begin{array}{r} 0(0.0) \\ 56(3.9) \\ 8(2.5) \\ 12(2.3) \\ 57(4.1) \end{array}$ | 494 (7.0) <br> 384 (33.0) <br> 483 (12.0) <br> 528 (7.7) | $\begin{array}{rr} 100 & (0.5) \\ 41 & (3.8) \\ 78 & (3.4) \\ 70 & (3.9) \\ 32 & (3.8) \end{array}$ | $\begin{aligned} & 537(7.2) \\ & 488(8.3) \\ & 343(7.1) \\ & 471(6.8) \\ & 513(8.5) \end{aligned}$ | $\begin{array}{r} 0(0.0) \\ 2(1.1) \\ 3(0.9) \\ 10(2.4) \\ 0(0.0) \end{array}$ | 361 (22.5) <br> 481 (15.3) |
| Singapore Slovak Republic Slovenia South Africa Thailand | $\begin{array}{r} 9(2.3) \\ 5(2.1) \\ 0(0.0) \\ 9(2.6) \\ 30(4.9) \end{array}$ | $\begin{gathered} 592(24.7) \\ 503(15.2) \\ \sim \\ \sim \\ 275(24.4) \\ 483(11.4) \end{gathered}$ | 37 (3.8) <br> 50 (4.8) <br> 26 (4.1) <br> 58 (4.2) <br> 9 (3.3) | $\begin{aligned} & 586 \text { (11.2) } \\ & 534 \text { (5.3) } \\ & 537(4.5) \\ & 277(8.8) \\ & 448(18.5) \end{aligned}$ | $\begin{array}{ll} 48 & (4.0) \\ 44 & (4.7) \\ 74 & (4.1) \\ 23 & (3.5) \\ 58 & (5.1) \end{array}$ | 623 (7.5) <br> 534 (6.1) <br> 528 (3.3) <br> 269 (13.3) <br> 461 (7.3) | $\begin{array}{r} 5(2.0) \\ 0(0.0) \\ 0(0.0) \\ 10(2.4) \\ 2(1.4) \end{array}$ | $\begin{aligned} 608 & (20.0) \\ \sim & \sim \\ \sim & \sim \\ 273 & (17.2) \\ \sim & \sim \end{aligned}$ |
| Tunisia <br> Turkey r <br> United States | $\begin{array}{r} 1(1.0) \\ 5(1.6) \\ 16(2.2) \end{array}$ | $\begin{aligned} & 418 \text { (16.3) } \\ & 490(9.2) \end{aligned}$ | $\begin{array}{r} 86(2.8) \\ 5(1.6) \\ 56(3.4) \end{array}$ | $\begin{aligned} & 448 \text { (2.8) } \\ & 415(10.5) \\ & 501(4.9) \end{aligned}$ | $\begin{aligned} & 12(2.6) \\ & 77(3.4) \\ & 17(2.6) \end{aligned}$ | $\begin{aligned} & 441(6.7) \\ & 429(5.0) \\ & 528(11.6) \end{aligned}$ | $\begin{array}{r} 1(1.0) \\ 13(2.7) \\ 11(2.3) \end{array}$ | $\begin{aligned} & 427 \text { (11.0) } \\ & 491 \text { (14.5) } \end{aligned}$ |
| International Avg. | 9 (0.3) | 481 (3.5) | 34 (0.5) | 492 (2.3) | 53 (0.5) | 490 (1.9) | 4 (0.3) | 485 (4.7) |

## Background data provided by teachers.

$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^8]|  | 5 Hours or More |  |  | 3.5 Hours to < 5 |  |  | 2 Hours to < 3.5 |  |  | Less Than 2 Hours |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students 1999 | $\begin{gathered} \text { 1995-1999 } \\ \text { Difference } \end{gathered}$ |  | Percent of Students 1999 | $\begin{aligned} & \text { 1995-1999 } \\ & \text { Difference } \end{aligned}$ |  | Percent of Students 1999 | $\begin{aligned} & \text { 1995-1999 } \\ & \text { Difference } \end{aligned}$ |  | Percent of Students 1999 | $\begin{aligned} & \text { 1995-1999 } \\ & \text { Difference } \end{aligned}$ |  |
| Australia | 3 (1.7) | 2 (1.8) | $\bullet$ | 44 (4.4) | -1 (6.4) | - | 50 (4.6) | -3 (6.7) | - | 3 (1.4) | 1 (1.7) | - |
| Belgium (Flemish) | 4 (1.0) | 4 (1.0) | - | 40 (2.8) | -10 (5.3) | - | 43 (3.8) | -7 (5.8) | - | 13 (3.4) | 13 (3.4) | $\triangle$ |
| Canada | 17 (2.2) | -1 (4.2) | $\bigcirc$ | 55 (3.2) | 6 (6.1) | - | 26 (2.7) | -5 (5.2) | - | 3 (0.9) | 0 (1.5) | - |
| Cyprus | $\mathrm{x} \times$ | $\mathrm{x} \times$ |  | $x \times$ | $x \times$ |  | x X | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ | $\mathrm{x} \times$ |  |
| Czech Republic | 4 (2.1) | 1 (2.6) | - | 52 (4.4) | -38 (5.2) | $\nabla$ | 44 (4.4) | 38 (4.8) | - | 0 (0.0) | -1 (0.9) | - |
| England | 2 (1.2) | 2 (1.2) | - | 3 (1.4) | -7 (3.1) | - | 95 (2.0) | 6 (3.4) | - | 0 (0.2) | -1 (0.9) |  |
| Hong Kong, SAR | 9 (2.3) | 2 (3.6) | - | 71 (4.0) | 9 (6.8) | - | 17 (3.1) | -9 (6.0) | - | 3 (1.5) | -2 (2.8) |  |
| Hungary | 3 (1.1) | 2 (1.5) | - | 15 (2.7) | -8 (4.6) | - | 80 (2.9) | 5 (4.8) | - | 1 (0.8) | 1 (0.8) |  |
| Iran, Islamic Rep. | -- | -- |  | - - | -- |  |  | -- |  |  | -- |  |
| Israel ${ }^{\dagger}$ | 4 (1.7) | -2 (4.0) | - | 63 (4.5) | 16 (9.4) | - | 30 (4.3) | -11 (9.7) | - | 3 (1.5) | -4 (4.2) |  |
| Italy | 9 (2.4) | -4 (4.5) | - | 56 (4.9) | 2 (7.1) | - | 30 (4.9) | 1 (6.6) | - | 5 (2.0) | 1 (2.7) |  |
| Japan | 1 (1.3) | 1 (1.3) | - | 2 (1.3) | -2 (2.1) | - | 95 (2.0) | 4 (3.1) | - | 2 (0.9) | -2 (2.0) |  |
| Korea, Rep. of | 2 (0.9) | -3 (2.5) | - | 3 (1.1) | -2 (2.0) | - | 93 (1.8) | 3 (3.3) | - | 3 (1.1) | 2 (1.2) | - |
| Latvia (LSS) | 7 (2.5) | -1 (3.5) | - | 62 (3.9) | 0 (5.6) | - | 31 (4.2) | 2 (5.8) | - | 0 (0.0) | -1 (0.1) | V |
| Lithuania | - - | -- |  | - - | -- |  | - - | - - |  | - - | - - |  |
| Netherlands | 0 (0.0) | - - | - | 0 (0.0) | -- | $\bullet$ | 100 (0.5) | 3 (2.0) | - | 0 (0.0) | -3 (1.9) | - |
| New Zealand | 1 (0.0) | -3 (1.5) | - | 56 (3.9) | 6 (5.7) | - | 41 (3.8) | -1 (5.6) | - | 2 (1.1) | -3 (2.1) | - |
| Romania | 9 (2.5) | 6 (3.1) | - | 12 (2.3) | 3 (3.3) | - | 70 (3.9) | -10 (5.2) | - | 10 (2.4) | 1 (3.5) | - |
| Russian Federation | 11 (2.5) | -2 (4.8) | - | 57 (4.1) | -12 (6.0) | - | 32 (3.8) | 15 (4.7) | $\triangle$ | 0 (0.0) | - - | - |
| Singapore | 9 (2.3) | 9 (2.3) | - | 37 (3.8) | -10 (6.0) | - | 48 (4.0) | -4 (6.1) | - | 5 (2.0) | 5 (2.0) | - |
| Slovak Republic | 5 (2.1) | -6 (3.6) | - | 50 (4.8) | -36 (5.7) | V | 44 (4.7) | 42 (4.9) | $\triangle$ | 0 (0.0) | -- | - |
| Slovenia | 0 (0.0) | -1 (0.8) | - | 26 (4.1) | 13 (5.3) | - | 74 (4.1) | -12 (5.3) | - | 0 (0.0) | -- | - |
| Thailand ${ }^{\dagger}$ | $\times \mathrm{x}$ | $\mathrm{x} \times$ |  | x x | x x |  | $\mathrm{x} \times$ | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ | $\mathrm{x} \times$ |  |
| United States | 16 (2.2) | 6 (3.3) | $\bullet$ | 56 (3.4) | -2 (5.8) | - | 17 (2.6) | -6 (4.6) | - | 11 (2.3) | 3 (3.2) | $\bullet$ |
| International Avg. ${ }^{\text {§ }}$ | 6 (0.4) | 1 (0.6) | - | 34 (0.7) | -7 (1.1) | V | 56 (0.8) | 5 (1.1) | $\triangle$ | 4 (0.4) | 2 (0.5) | $\triangle$ |

A 1999 significantly higher than 1995

- No significant difference between 1995 and 1999
- 1999 significantly lower than 1995

Significance tests adjusted for multiple comparisons

Background data provided by teachers.
† Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.
Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash ( - ) indicates data are not available.
An " $r$ " indicates teacher response data available for $70-84 \%$ of students, based on the lower response rate in either 1995 or 1999. An " " " indicates teacher response data available for $<50 \%$ of students, based on the lower response rate in either 1995 or 1999.

|  | Never |  | Once in a While |  | Pretty Often |  | Almost Always |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Australia Belgium (Flemish) Bulgaria Canada Chile | $\begin{array}{r} 11(0.7) \\ 24(1.1) \\ 19(0.9) \\ 9(0.4) \\ 18(0.7) \end{array}$ | $\begin{aligned} & 523(8.2) \\ & 557(5.9) \\ & 511(7.5) \\ & 528(4.2) \\ & 395(8.5) \end{aligned}$ | 66 (1.1) <br> 62 (1.1) <br> 64 (1.2) <br> 64 (1.0) <br> 49 (0.8) | 534 (5.0) 566 (2.9) 522 (5.1) 540 (2.4) 407 (4.8) | 16 (0.8) <br> 9 (0.7) <br> 10 (0.9) <br> 18 (0.7) <br> 17 (0.6) | $\begin{aligned} & 510(7.9) \\ & 562 \text { (6.8) } \\ & 506 \text { (13.9) } \\ & 517 \text { (3.9) } \\ & 384(5.5) \end{aligned}$ | $\begin{array}{r} 7(0.7) \\ 5(0.8) \\ 7(0.6) \\ 9(0.7) \\ 16(0.7) \end{array}$ | $\begin{aligned} & 485(8.3) \\ & 505(20.3) \\ & 456(10.7) \\ & 502(7.8) \\ & 362(6.6) \end{aligned}$ |
| Chinese Taipei Cyprus Czech Republic England Finland | $\begin{array}{ll} 22 & (1.1) \\ 26 & (1.0) \\ 33 & (1.7) \\ 10 & (0.8) \\ 34 & (1.3) \end{array}$ | 580 (6.1) <br> 479 (3.9) <br> 520 (4.0) <br> 508 (9.5) <br> 526 (3.6) | 56 (1.0) 49 (1.0) 59 (1.3) 66 (1.2) 57 (1.3) | $\begin{aligned} & 594(4.4) \\ & 485(2.2) \\ & 524(4.7) \\ & 509(4.2) \\ & 523(3.2) \end{aligned}$ | $\begin{array}{r} 17(0.9) \\ 19(0.9) \\ 4(0.5) \\ 19(1.1) \\ 6(0.6) \end{array}$ | $\begin{aligned} & 580(5.4) \\ & 470(4.9) \\ & 517(11.4) \\ & 474(6.0) \\ & 502(7.1) \end{aligned}$ | $\begin{aligned} & 6(0.6) \\ & 5(0.5) \\ & 4(0.8) \\ & 6(0.6) \\ & 3(0.3) \end{aligned}$ | $\begin{aligned} & 563 \text { (9.0) } \\ & 434 \text { (8.6) } \\ & 472 \text { (13.7) } \\ & 437 \text { (8.9) } \\ & 473 \text { (10.4) } \end{aligned}$ |
| Hong Kong, SAR Hungary Indonesia Iran, Islamic Rep. Israel | 36 (1.0) <br> 46 (1.5) <br> 15 (1.0) <br> 33 (1.2) <br> 20 (1.0) | $\begin{aligned} & 585(4.4) \\ & 541(4.3) \\ & 386(8.2) \\ & 425(4.2) \\ & 457(7.7) \end{aligned}$ | 54 (0.8) 45 (1.3) 75 (1.1) 39 (1.0) 47 (1.3) | $\begin{aligned} & 588(4.0) \\ & 528(4.3) \\ & 413(4.6) \\ & 435(4.2) \\ & 485(3.7) \end{aligned}$ | $\begin{array}{r} 8(0.6) \\ 5(0.4) \\ 8(0.6) \\ 15(0.8) \\ 20(0.8) \end{array}$ | $\begin{aligned} & 552(8.9) \\ & 497(7.8) \\ & 378(9.6) \\ & 404(6.4) \\ & 469(5.2) \end{aligned}$ | $\begin{array}{r} 2(0.2) \\ 4(0.4) \\ 2(0.2) \\ 14(0.6) \\ 13(0.7) \end{array}$ | 515 (13.5) <br> 414 (6.2) <br> 446 (7.3) |
| Italy Japan Jordan Korea, Rep. of Latvia (LSS) | 16 (1.0) <br> 53 (1.4) <br> 29 (1.0) <br> 57 (0.9) <br> 39 (1.3) | 480 (5.5) 580 (2.7) 440 (5.2) 581 (2.0) 501 (4.6) | 54 (1.2) <br> 42 (1.3) <br> 39 (0.9) <br> 38 (0.8) <br> 52 (1.3) | 488 (4.0) <br> 581 (2.5) <br> 455 (4.3) <br> 598 (3.0) <br> 513 (3.9) | $\begin{array}{r} 18(1.0) \\ 4(0.3) \\ 19(0.7) \\ 4(0.2) \\ 5(0.5) \end{array}$ | 477 (5.3) <br> 559 (5.9) <br> 414 (4.8) <br> 579 (7.5) <br> 491 (8.6) | $\begin{array}{r} 11(0.8) \\ 1(0.2) \\ 14(0.8) \\ 1(0.1) \\ 3(0.4) \end{array}$ | $\begin{gathered} 450(7.6) \\ \sim \sim \\ 403(6.8) \\ \sim \sim \\ \sim \\ \sim 1 \\ \sim \end{gathered}$ |
| Lithuania ${ }^{\ddagger}$ <br> Macedonia, Rep. of <br> Malaysia <br> Moldova <br> Morocco | 33 (1.3) <br> 32 (1.1) <br> 32 (1.5) <br> 34 (1.3) | $\begin{gathered} -- \\ 464(4.5) \\ 509(5.2) \\ 478(5.9) \\ 350(4.7) \end{gathered}$ | 48 (1.1) <br> 60 (1.0) <br> 50 (1.5) <br> 26 (1.1) | $\begin{gathered} -- \\ 464(5.2) \\ 525(4.4) \\ 477(4.3) \\ 355(4.2) \end{gathered}$ | 10 (0.6) <br> 7 (0.5) <br> 10 (0.6) <br> 23 (0.8) | $\begin{gathered} -- \\ 416(7.0) \\ 526(7.8) \\ 450(6.2) \\ 331(5.9) \end{gathered}$ | $\begin{aligned} & -- \\ & 9(0.6) \\ & 2(0.2) \\ & 8(0.6) \\ & 16(0.8) \end{aligned}$ | 404 (9.2) <br> 434 (7.4) <br> 322 (8.7) |
| Netherlands New Zealand Philippines Romania Russian Federation | $\begin{array}{r} 39(1.3) \\ 7(0.5) \\ 14(0.6) \\ 38(1.7) \\ 17(1.5) \end{array}$ | $\begin{array}{ll} 539 & (7.7) \\ 474 & (10.9) \\ 351 & (8.3) \\ 481 & (5.7) \\ 538 & (11.1) \end{array}$ | $\begin{array}{ll} 55 & (1.3) \\ 53 & (1.3) \\ 36 & (1.1) \\ 50 & (1.6) \\ 64 & (1.5) \end{array}$ | 544 (8.3) <br> 515 (4.9) <br> 368 (7.2) <br> 481 (5.8) <br> 533 (5.2) | $\begin{array}{r} 4(0.5) \\ 27(1.0) \\ 25(0.7) \\ 7(0.6) \\ 10(0.9) \end{array}$ | $\begin{aligned} & 524(14.0) \\ & 481(6.1) \\ & 344 \text { (7.7) } \\ & 450(11.0) \\ & 506(7.5) \end{aligned}$ | $\begin{array}{r} 2(0.4) \\ 13(0.8) \\ 25(1.1) \\ 5(0.5) \\ 9(0.7) \end{array}$ | 440 (8.3) <br> 320 (7.2) <br> 417 (13.0) <br> 497 (6.9) |
| Singapore <br> Slovak Republic Slovenia South Africa Thailand | $\begin{array}{r} 16(0.8) \\ 37(1.3) \\ 9(0.9) \\ 24(1.2) \\ 23(0.8) \end{array}$ | $\begin{aligned} & 592(8.9) \\ & 534(4.7) \\ & 504(6.6) \\ & 261(6.2) \\ & 453(5.7) \end{aligned}$ | 64 (1.0) <br> 55 (1.1) <br> 58 (1.2) <br> 27 (1.2) <br> 65 (1.0) | $\begin{array}{ll} 614(5.9) \\ 537 & (4.3) \\ 541 & (2.8) \\ 323 & (10.4) \\ 478 & (5.3) \end{array}$ | $\begin{array}{r} 14(0.6) \\ 6(0.7) \\ 20(0.9) \\ 23(0.6) \\ 9(0.6) \end{array}$ | $\begin{aligned} & 585 \text { (7.4) } \\ & 515 \text { (13.0) } \\ & 530(4.7) \\ & 269 \text { (10.0) } \\ & 447(8.4) \end{aligned}$ | $\begin{array}{r} 6(0.4) \\ 2(0.3) \\ 12(0.7) \\ 26(0.9) \\ 3(0.3) \end{array}$ | $579(9.5)$ $\sim \sim$ $\sim 06(6.8)$ $251(6.3)$ $427(12.3)$ |
| Tunisia <br> Turkey <br> United States | $\begin{aligned} & 63(0.9) \\ & 49 \\ & 10 \\ & 10 \end{aligned}(0.4)$ | $\begin{aligned} & 451(2.5) \\ & 445(4.1) \\ & 494(8.2) \end{aligned}$ | $\begin{array}{ll} 23 & (0.7) \\ 40 & (1.0) \\ 59 & (0.9) \end{array}$ | $\begin{aligned} & 451(3.3) \\ & 430(5.0) \\ & 522(3.9) \end{aligned}$ | $\begin{array}{r} 7(0.4) \\ 6(0.4) \\ 20(0.5) \end{array}$ | $\begin{aligned} & 433(6.5) \\ & 396(7.7) \\ & 488(3.9) \end{aligned}$ | $\begin{array}{r} 7(0.4) \\ 5(0.5) \\ 11(0.6) \end{array}$ | $\begin{aligned} & 432 \text { (7.6) } \\ & 374 \text { (11.1) } \\ & 455 \text { (5.1) } \end{aligned}$ |
| International Avg. | 28 (0.2) | 487 (1.2) | 52 (0.2) | 499 (0.8) | 13 (0.1) | 474 (1.4) | 8 (0.1) | 442 (1.8) |

[^9][^10]
## What Activities Do Students Do in Their Mathematics Lessons?

Because it can affect pedagogical strategies, class size data are shown in

"Exhibit 6.8. Teachers' reports about the size of their eighth-grade mathematics class reveal that across countries the average class size was 31 students, but there was considerable variation - from more than 50 students in the Philippines and South Africa to fewer than 20 students in Belgium (Flemish) and Finland. The relationship between class size and achievement is difficult to disentangle, given the variety of policies and practices and the fact that smaller classes can be used for both advanced and remedial learning. As shown in Exhibit 6.9, Cyprus, Korea, and Slovenia significantly reduced the average size of their mathematics classes between 1995 and 1999, and no countries showed increases.

Exhibit 6.1o presents a profile of the activities most commonly encountered in mathematics classes around the world, as reported by mathematics teachers. The two predominant activities, accounting for nearly half of class time on average, were teacher lecture ( 23 percent of class time) and teacher-guided student practice ( 22 percent). As shown in Exhibit 6.11, most students ( 86 percent on average internationally) agreed with teachers' reports, saying that their teachers frequently showed them how to do mathematics problems. According to 55 to 59 percent of the students, discussing homework and working independently on worksheets or textbooks were also frequent activities in class. Students also reported that use of the board was an extremely common presentational mode (see Exhibit 6.12). On average internationally, 92 percent of students reported that teachers used the board at least pretty often, and 60 percent reported that students used it at least pretty often. The use of an overhead projector was a popular presentational mode for teachers in some countries, with more than $4^{\circ}$ percent of the students in Canada, Finland, Singapore, South Africa, and the United States reporting that their teachers use it at least pretty often.

Educators, parents, employers, and most of the public support the goal of improving students' capacity for mathematics problem-solving. To examine the emphasis placed on that goal, timss created an index of teachers' emphasis on mathematics reasoning and problem-solving (EMRPS). As shown in Exhibit 6.13, the index is based on teachers' responses about how often they asked students to explain the reasoning behind an idea, represent and analyze relationships using tables, charts, or graphs, work on problems for which there was no immediate solution, and write equations to represent relationships. Students were placed in the high category if, on
average, they were asked to do these activities in most of their lessons. The medium level represents students asked to do these activities in some to most lessons, and students in the low category did the activities only in some lessons or rarely.

Nearly half the Japanese students were at the high level, compared with the international average of 15 percent. Across countries, most students ( 61 percent on average) were in the medium category. Countries with more than 70 percent of their students in the medium category were Romania, Slovenia, Bulgaria, the Czech Republic, the Slovak Republic, Hungary, Moldova, and the Russian Federation. Emphasizing reasoning and problem-solving was related to performance, with students at the high and medium levels having higher average achievement than those at the low level, both internationally and for most countries.

Exhibit R3.9 in the reference section shows the percentages of students asked in most or every lesson to engage in each of the activities included in the problem-solving index. For comparison purposes the percentages of students asked to practice computational skills in most or every lesson are also shown. According to their teachers, internationally on average, nearly three-fourths of the students (73 percent) were asked to practice their computational skills in most or every mathematics lesson. Nearly as many ( 7 o percent) were asked to explain the reasoning behind an idea this frequently. The other three problem-solving activities occurred much less often. Forty-three percent of students, on average across countries, wrote equations representing relationships in most or every lesson, but only about one-fourth ( 26 percent) represented and analyzed relationships using tables or graphs, and about one-fifth ( 21 percent) worked on problems for which there was no immediately obvious method of solution.

Exhibit 6.14 shows trend data for the index of teachers' emphasis on mathematics reasoning and problem-solving. These data suggest
 increased emphasis on problem-solving activities since the first timss assessment. Between 1995 and 1999, there was a small but significant increase (four percent) in the percentage of students at the high index level. Among countries, only Canada showed a significant increase, as the percentage of Canadian students in the high category rose from 4 to 13 percent. As shown in Exhibit R3.10 in the reference section, the international averages for the percentages of students asked to do the activities in most or every mathematics lesson increased for three of the activities (all except explain the rea-
soning behind an idea, which already was very frequent). Interestingly, however, the percentage of students asked to practice their computational skills in most or every lesson also increased significantly between 1995 and 1999.

Teachers were not asked about the emphasis placed on using things from everyday life in solving mathematics problems, but students were (see Exhibit R3.11). In most of the countries, students reported a moderate emphasis on doing these types of problems in mathematics class. Nearly two-thirds ( 65 percent), on average internationally, said these activities occurred once in a while or pretty often, and an additional 15 percent said they occurred almost always.


[^11]An " $r$ " indicates teacher response data available for $70-84 \%$ of students. An " $s$ " indicates teacher response data available for $50-69 \%$ of students. An "x" indicates teacher response data available for $<50 \%$ of students.

|  | Overall Average Class Size |  |  | 1-20 Students |  |  | 21-35 Students |  |  | 36 or More Students |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Average | 1995-1999 Differenc |  | Percent of Students 1999 | 1995-199 <br> Differenc |  | Percent of Students 1999 | 1995-199: Differenc |  | Percent of Students 1999 | 1995-199 <br> Differenc |  |
| Australia | 27 (0.3) | 1 (0.5) | - | 9 (2.4) | -4 (3.3) | - | 91 (2.4) | 5 (3.4) | - | 0 (0.0) | -1 (0.8) | - |
| Belgium (Flemish) | 19 (0.4) | -1 (0.5) | - | 58 (3.5) | 9 (5.0) | $\bullet$ | 42 (3.5) | -9 (5.0) | - | 0 (0.0) | - - | - |
| Canada | 27 (0.3) | 0 (0.5) | - | 11 (2.1) | 0 (3.0) | $\bullet$ | 87 (2.3) | 0 (3.3) | - | 2 (1.0) | 0 (1.4) | - |
| Cyprus | 29 (0.2) | -2 (0.5) | $\checkmark$ | 0 (0.2) | -1 (0.7) | $\bullet$ | 100 (0.2) | 1 (0.7) | $\bullet$ | 0 (0.0) | - - | $\bullet$ |
| Czech Republic | 24 (0.4) | -1 (0.6) | - | 18 (4.2) | 5 (5.3) | - | 82 (4.2) | -5 (5.3) | - | 0 (0.0) | -- | - |
| England | $x$ x | $x \mathrm{x}$ |  | x x | $x$ x |  | x x | x x |  | x x | x x |  |
| Hong Kong, SAR | 37 (0.5) | -1 (0.8) | $\bullet$ | 7 (1.8) | 3 (2.6) | $\bullet$ | 15 (3.0) | 7 (4.3) | $\bullet$ | 78 (3.4) | -10 (4.9) | - |
| Hungary | 21 (0.5) | -1 (0.7) | - | 48 (4.2) | 11 (6.1) | - | 51 (4.1) | -10 (6.2) | - | 1 (0.0) | -1 (1.1) | - |
| Iran, Islamic Rep. | 33 (0.5) | -3 (1.3) | - | 5 (1.6) | 4 (1.8) | - | 57 (4.2) | 5 (7.2) | $\bullet$ | 38 (4.2) | -9 (7.2) | - |
| Israel ${ }^{\dagger}$ | 25 (0.8) | -4 (1.5) | - | 34 (3.7) | 21 (5.6) | $\triangle$ | 48 (4.4) | -13 (8.8) | - | 18 (3.5) | -8 (7.9) | - |
| Italy | 20 (0.4) | 1 (0.6) | - | 53 (4.8) | -11 (6.9) | - | 47 (4.7) | 10 (6.8) | - | 1 (0.0) | 1 (0.0) | $\triangle$ |
| Japan | 36 (0.2) | -1 (0.4) | - | 1 (0.0) | 0 (0.0) | $\triangle$ | 41 (3.4) | 8 (5.3) | $\bullet$ | 58 (3.3) | -9 (5.3) | - |
| Korea, Rep. of | 42 (0.5) | -8 (0.9) | V | 0 (0.0) | -2 (1.4) | $\bullet$ | 12 (2.2) | 10 (2.6) | - | 88 (2.2) | -7 (2.9) | - |
| Latvia (LSS) | 22 (0.5) | 0 (1.0) | - | 45 (4.2) | 4 (7.1) | $\bullet$ | 55 (4.2) | 1 (7.3) | - | 0 (0.0) | -5 (2.1) | - |
| Lithuania | 23 (0.3) | 2 (0.6) | - | 32 (2.8) | -11 (5.8) | - | 68 (2.8) | 11 (5.8) | - | 0 (0.0) | - - | - |
| Netherlands | 25 (0.5) | 0 (0.8) | - | 13 (4.1) | -3 (6.4) | - | 87 (4.1) | 3 (6.4) | - | 0 (0.0) | - - | - |
| New Zealand | 25 (0.4) | -1 (0.6) | - | 17 (2.9) | 6 (4.0) | $\bullet$ | 82 (2.8) | -7 (4.0) | - | 1 (0.0) | 1 (0.0) | $\triangle$ |
| Romania | 24 (0.4) | -2 (0.9) | - | 30 (2.9) | 7 (5.2) | - | 65 (3.2) | -1 (5.4) | $\bullet$ | 5 (1.9) | -5 (3.6) | - |
| Russian Federation | 24 (0.5) | -1 (0.6) | - | 19 (3.2) | 4 (4.2) | - | 81 (3.2) | -3 (4.3) | - | 0 (0.0) | -1 (0.2) | V |
| Singapore | 37 (0.3) | 0 (0.5) | - | 1 (0.4) | 0 (0.8) | - | 32 (3.8) | -1 (5.8) | $\bullet$ | 68 (3.8) | 1 (5.8) | - |
| Slovak Republic | 25 (0.4) | -1 (0.5) | $\bigcirc$ | 15 (2.6) | 0 (3.8) | - | 85 (2.6) | 0 (3.9) | - | 0 (0.2) | 0 (0.8) | - |
| Slovenia | 22 (0.3) | -2 (0.4) | $\checkmark$ | 29 (3.2) | 13 (4.4) | - | 71 (3.2) | -13 (4.4) | $\bullet$ | 0 (0.0) | - - | - |
| Thailand ${ }^{\dagger}$ | x x | x x |  | $x \mathrm{x}$ | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ | $\mathrm{x} \times$ |  | $\mathrm{x} \times$ | x x |  |
| United States | 26 (0.7) | 1 (1.0) | - | 21 (2.6) | -4 (4.3) | $\bullet$ | 73 (3.0) | 3 (4.7) | $\bullet$ | 6 (1.4) | 1 (2.3) | - |
| International Avg. § | 27 (0.1) | -1 (0.2) | v | 21 (0.6) | 2 (0.9) | - | 63 (0.7) | 0 (1.1) | $\bullet$ | 16 (0.4) | -1 (0.6) | - |



## Background data provided by teachers.

$\dagger$ Countries with unapproved sampling procedures at the classroom level in 1995
§ International average is for countries that participted and met sampling guidelines in both 1995 and 1999
Trend notes: Because coverage fell below $65 \%$ in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates data are not available.
An " $r$ " indicates teacher response data available for $70-84 \%$ of students, based on the lower response rate in either 1995 or 1999. An " $s$ " indicates teacher response data available for $50-69 \%$ of students, based on the lower response rate in either 1995 or 1999. An "x" indicates teacher response data available for $<50 \%$ of students, based on the lower response rate in either 1995 or 1999.

\begin{tabular}{|c|c|c|c|c|c|c|c|c|}
\hline \& \multicolumn{8}{|c|}{Average Percentage of Class Time Spent in a Typical Month of Lessons} \\
\hline \& Administrative Tasks \& Homework Review \& Lecture-Style Presentation by Teacher \& TeacherGuided Student Practice \& Re-teaching and Clarification of Content/ Procedures \& Student Independent Practice \& Tests and Quizzes \& Other \\
\hline \begin{tabular}{l}
Australia Belgium (Flemish) \\
Bulgaria \\
Canada Chile
\end{tabular} \& \[
\begin{array}{r} 
\\
4(0.4) \\
\\
\\
\\
\\
r \\
2(0.3) \\
\\
\\
\\
5(0.4) \\
6(0.2)
\end{array}
\] \& \(9(0.5)\)
\(7(0.4)\)
\(7(0.4)\)
\(r \quad 14(0.4)\)

$14(0.6)$ \& $19(1.3)$
$24(1.1)$
$37(1.7)$
$r \quad 20(0.9)$
$24(1.2)$ \& $22(0.9)$
$29(1.0)$
$18(1.1)$
$r \quad 18(0.8)$

$18(0.9)$ \& $$
\begin{array}{r}
12(0.6) \\
10(0.4) \\
\\
r \\
10(0.5) \\
r \\
\\
10(0.3) \\
19(0.8)
\end{array}
$$ \& $22(1.3)$

$14(0.9)$
$14(1.3)$
$r \quad 20(0.7)$
$8(0.5)$ \& $8(0.3)$

$r$
$10(0.3)$
$10(0.6)$

$12(0.3)$
$(0.6)$ \& $3(0.4)$

$1(0.4)$

$3(0.3)$

$3(0.6)$ <br>

\hline | Chinese Taipei |
| :--- |
| Cyprus |
| Czech Republic |
| England Finland | \& \[

$$
\begin{array}{ll} 
& 3(0.6) \\
& 3(0.4) \\
& 3(0.3) \\
& 3(0.2) \\
& 2(0.3)
\end{array}
$$

\] \& |  | $12(0.5)$ |
| ---: | ---: |
| $r$ | $21(0.8)$ |
|  | $5(0.4)$ |
| s | $6(0.5)$ |
|  | $16(0.6)$ | \& |  | $39(1.3)$ |
| ---: | ---: |
| $r$ | $17(1.0)$ |
|  | $23(0.7)$ |
| s | $18(0.9)$ |
|  | $15(0.7)$ | \& \[

$$
\begin{array}{rl} 
& 15(0.5) \\
\mathrm{r} & 25(1.0) \\
& 29(1.2) \\
\mathrm{s} & 27(1.2) \\
& 25(1.1)
\end{array}
$$

\] \& \[

$$
\begin{array}{rl} 
& 11(0.6) \\
r & 12(0.5) \\
& 10(0.5) \\
& 11(0.4) \\
& 10(0.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{rr} 
& 9(0.5) \\
r & 10(1.0) \\
& 19(1.0) \\
\text { s } & 24(1.5) \\
& 24(1.4)
\end{array}
$$

\] \&  \& \[

$$
\begin{array}{ll} 
& 2(0.4) \\
& \begin{array}{l}
2(0.3) \\
\\
\\
\\
\\
\\
3(0.4) \\
\\
3(0.7) \\
2(0.3)
\end{array}
\end{array}
$$
\] <br>

\hline | Hong Kong, SAR |
| :--- |
| Hungary |
| Indonesia |
| Iran, Islamic Rep. |
| Israel | \& \[

$$
\begin{aligned}
& 5(0.7) \\
& 2(0.2) \\
& 7(0.5) \\
& 6(0.9) \\
& 4(0.6)
\end{aligned}
$$

\] \& \[

$$
\begin{array}{r}
12(0.7) \\
\\
\\
\\
\\
\\
\\
\\
\\
\\
r \\
r
\end{array}
$$ 15(0.5)
\] \& $32(1.6)$

$14(0.7)$
$11(1.0)$
$25(2.4)$

$r \quad 19(0.8)$ \& \[
$$
\begin{array}{r} 
\\
\\
\\
\\
29(0.8) \\
\\
\\
29(1.0) \\
\\
\\
r
\end{array}
$$ 21(2.6)

\] \& \[

$$
\begin{array}{r}
8(0.4) \\
\\
\\
\\
13(0.5) \\
\\
13(0.6) \\
\\
r \quad 22(2.6) \\
r
\end{array}
$$ 14(0.8)

\] \&  \& \[

$$
\begin{array}{r}
8(0.4) \\
\\
\\
\\
\\
\\
16(0.4) \\
\\
r \quad 22(0.9) \\
r \quad 10(0.5)
\end{array}
$$

\] \& \[

$$
\begin{array}{r} 
\\
3(0.4) \\
\\
3(0.4) \\
\\
4(0.4) \\
\\
\\
\hline
\end{array}
$$
\] <br>

\hline | Italy |
| :--- |
| Japan Jordan |
| Korea, Rep. of Latvia (LSS) | \& \[

$$
\begin{array}{ll}
2(0.2) \\
2(0.5) \\
8(1.0) \\
3(0.6) \\
3(0.2)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
14(0.5) \\
5(0.4) \\
18(1.2) \\
6(0.3) \\
11(0.7)
\end{array}
$$

\] \& | 25 (0.7) |
| :--- |
| 34 (1.6) |
| 18 (1.4) |
| 33 (1.4) |
| 16 (0.9) | \& \[

$$
\begin{aligned}
& 22(0.7) \\
& 26(1.3) \\
& 22(1.5) \\
& 22(0.8) \\
& 33(1.6)
\end{aligned}
$$

\] \& \[

$$
\begin{aligned}
& 13(0.4) \\
& 16 \\
& (0.9) \\
& 14 \\
& (1.1) \\
& 14 \\
& (0.8) \\
& 13
\end{aligned}
$$(0.8)

\] \& | 12 (0.5) |
| :--- |
| 9 (0.7) |
| 16 (1.3) |
| 14 (0.8) |
| 10 (0.9) | \& \[

$$
\begin{array}{r}
12(0.5) \\
7(0.5) \\
15(1.2) \\
7(0.3) \\
7(0.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
1 & (0.2) \\
2 & (0.3) \\
6 & (0.9) \\
3 & (0.4) \\
7 & (0.8)
\end{array}
$$
\] <br>

\hline | Lithuania ${ }^{\ddagger}$ |
| :--- |
| Macedonia, Rep. of |
| Malaysia |
| Moldova |
| Morocco | \& \[

$$
\begin{array}{ll}
2 & (0.2) \\
5 & (0.3) \\
7 & (0.7) \\
5 & (1.1) \\
3 & (0.3)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
8(0.4) \\
8(0.4) \\
17(1.0) \\
15(1.0) \\
14(0.6)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
22 & (0.7) \\
41 & (1.2) \\
19 & (1.1) \\
21 & (1.1) \\
28 & (1.1)
\end{array}
$$

\] \& \[

$$
\begin{aligned}
& 26(1.0) \\
& 18(0.8) \\
& 27(1.3) \\
& 20(0.9) \\
& 19(1.0)
\end{aligned}
$$

\] \& \[

$$
\begin{array}{r}
10(0.3) \\
7(0.4) \\
13(0.8) \\
11(0.5) \\
12(0.8)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
14(0.6) \\
11(0.5) \\
11(0.9) \\
18(0.9) \\
5(0.6)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
13(0.5) \\
7(0.4) \\
10(0.5) \\
9(0.5) \\
12(0.7)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
2 & (0.3) \\
3 & (0.3) \\
4 & (0.5) \\
5 & (0.5) \\
5 & (0.7)
\end{array}
$$
\] <br>

\hline Netherlands
New Zealand
Philippines
Romania

Russian Federation \& $$
\begin{aligned}
& 5(0.4) \\
& 5(0.3) \\
& 8(1.1) \\
& 4(0.5) \\
& 2(0.1)
\end{aligned}
$$ \& \[

$$
\begin{array}{r}
15(1.5) \\
9(0.4) \\
12(1.0) \\
12(0.4) \\
10(0.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
9(1.2) \\
17(0.9) \\
24(1.4) \\
26(1.2) \\
25(0.6)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
5(1.0) \\
22(1.1) \\
19(1.2) \\
16(0.8) \\
17(0.7)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
18 & (1.1) \\
11 & (0.6) \\
13 & (1.0) \\
12 & (0.6) \\
11 & (0.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{ll}
32 & (2.0) \\
24 & (1.2) \\
18 & (1.2) \\
12 & (0.5) \\
17 & (0.6)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
11(0.6) \\
8(0.3) \\
18(1.1) \\
14(0.7) \\
12(0.6)
\end{array}
$$

\] \& \[

$$
\begin{aligned}
& 5(1.0) \\
& 3(0.5) \\
& 4(0.5) \\
& 4(0.4) \\
& 5(0.4)
\end{aligned}
$$
\] <br>

\hline Singapore Slovak Republic Slovenia South Africa Thailand \& $$
\begin{array}{r}
6(0.6) \\
3(0.3) \\
4(0.3) \\
13(1.4) \\
10
\end{array}
$$ \& \[

$$
\begin{array}{r}
13(0.7) \\
8(0.3) \\
11(0.5) \\
26(1.6) \\
16
\end{array}
$$(1.2)

\] \& \[

$$
\begin{array}{r}
28(1.5) \\
9(0.8) \\
24(1.0) \\
23(1.8) \\
22(1.5)
\end{array}
$$

\] \& \[

$$
\begin{aligned}
& 20(1.2) \\
& 30(1.1) \\
& 24(0.8) \\
& 26(1.7) \\
& 19(1.1)
\end{aligned}
$$

\] \& \[

$$
\begin{array}{r}
9(0.3) \\
13(0.5) \\
16(0.7) \\
21(1.6) \\
15(1.0)
\end{array}
$$

\] \& \[

$$
\begin{aligned}
& 12(0.8) \\
& 23(1.1) \\
& 10(0.7) \\
& 21(1.8) \\
& 16 \\
& 16
\end{aligned}
$$

\] \& \[

$$
\begin{array}{r}
8(0.4) \\
11(0.5) \\
8(0.3) \\
22(1.3) \\
14(1.1)
\end{array}
$$

\] \& \[

$$
\begin{aligned}
& 3(0.3) \\
& 4(0.5) \\
& 3(0.4) \\
& 7(1.1) \\
& 3(0.5)
\end{aligned}
$$
\] <br>

\hline | Tunisia |
| :--- |
| Turkey |
| United States | \& \[

$$
\begin{array}{r}
3(0.3) \\
\\
\\
\mathrm{r}(0.6) \\
6(0.3)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
14(0.8) \\
9(0.7) \\
r \quad 15(0.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
20(1.7) \\
\\
49(1.2) \\
r \quad 20(0.7)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
27(1.4) \\
14(0.8) \\
r \quad 18(0.4)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
11(0.7) \\
13(0.8) \\
r \quad 12(0.5)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
8(0.7) \\
\\
r \quad 17(0.7) \\
r(0.9)
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
12(0.7) \\
\\
\\
r \quad 11(0.6) \\
\hline
\end{array}
$$

\] \& \[

$$
\begin{array}{r}
4(0.4) \\
\\
4(0.6) \\
r \quad 4(0.5)
\end{array}
$$
\] <br>

\hline International Avg. \& 5 (0.1) \& 12 (0.1) \& 23 (0.2) \& 22 (0.2) \& 13 (0.1) \& 15 (0.2) \& 11 (0.1) \& 4 (0.1) <br>
\hline
\end{tabular}

$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
() Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

An " r " indicates teacher response data available for $70-84 \%$ of students. An " s " indicates teacher response data available for $50-69 \%$ of students.

|  | Percentage of Students Reporting Almost Always or Pretty Often |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | We Discuss Our Completed Homework | Teacher Shows Us How to Do Mathematics | We Work on Worksheets or Textbooks on Our | We Work on Mathematics Projects | We Begin Our Homework |
| Australia | 44 (1.8) | 93 (0.7) | 91 (1.2) | 25 (1.7) | 56 (1.6) |
| Belgium (Flemish) | 43 (1.4) | 69 (0.9) | 64 (1.0) | 16 (1.1) | 20 (1.4) |
| Bulgaria | 48 (1.9) | 89 (1.0) | 32 (1.2) | 15 (1.0) | 21 (1.4) |
| Canada | 62 (1.4) | 92 (0.5) | 92 (0.5) | 28 (1.1) | 82 (1.2) |
| Chile | 47 (1.3) | 89 (0.9) | 40 (1.1) | 46 (1.6) | 55 (1.2) |
| Chinese Taipei | 55 (1.0) | 91 (0.5) | 59 (1.2) | 55 (1.2) | 34 (1.0) |
| Cyprus | 72 (1.1) | 92 (0.7) | 67 (1.0) | 29 (1.0) | 52 (2.3) |
| Czech Republic | 42 (1.8) | 86 (1.1) | 51 (2.4) | 8 (0.6) | 16 (1.6) |
| England | 62 (1.5) | 93 (0.7) | 88 (1.5) | 35 (1.4) | 27 (1.6) |
| Finland | 37 (1.3) | 67 (1.3) | 90 (1.0) | 7 (0.8) | 47 (2.0) |
| Hong Kong, SAR | 35 (1.1) | 91 (0.6) | 69 (1.2) | 67 (1.4) | 40 (1.1) |
| Hungary | 71 (1.5) | 87 (1.0) | 63 (1.7) | 96 (0.4) | 18 (1.2) |
| Indonesia | 48 (1.0) | 88 (0.6) | 36 (1.5) | 86 (0.9) | 13 (0.7) |
| Iran, Islamic Rep. | 56 (1.0) | 82 (0.7) | 45 (0.9) | 30 (1.1) | 34 (1.3) |
| Israel | 64 (1.3) | 90 (0.6) | 72 (1.2) | 20 (1.0) | 65 (1.5) |
| Italy | 64 (1.4) | 80 (1.2) | 34 (1.2) | 22 (1.3) | 39 (2.3) |
| Japan | 19 (1.2) | 88 (0.7) | 38 (1.5) | 6 (0.7) | 20 (1.3) |
| Jordan | 76 (0.9) | 92 (0.6) | 45 (1.1) | 40 (1.4) | 59 (1.1) |
| Korea, Rep. of | 10 (0.5) | 85 (0.8) | 29 (0.7) | 46 (1.2) | 17 (0.7) |
| Latvia (LSS) | 48 (1.8) | 86 (1.0) | 54 (1.2) | - - | 28 (1.6) |
| Lithuania ${ }^{\text {\# }}$ | - - | - - | -- | - - | - - |
| Macedonia, Rep. of | 72 (1.3) | 86 (0.8) | 66 (1.6) | 37 (1.1) | 30 (1.4) |
| Malaysia | 61 (1.0) | 92 (0.5) | 13 (0.7) | 68 (1.1) | 67 (1.3) |
| Moldova | 61 (1.3) | 91 (0.8) | 66 (1.7) | 52 (1.6) | 32 (1.6) |
| Morocco | 69 (0.8) | 86 (0.6) | 53 (1.0) | 49 (1.1) | 53 (1.2) |
| Netherlands | 68 (3.7) | 70 (2.7) | 92 (1.1) | 3 (0.7) | 89 (1.5) |
| New Zealand | 55 (1.8) | 92 (0.6) | 89 (1.0) | 33 (1.5) | 43 (1.7) |
| Philippines | 78 (0.8) | 87 (0.8) | 64 (1.0) | 56 (1.2) | 49 (1.1) |
| Romania | 62 (1.4) | 83 (0.9) | 49 (1.1) | 38 (2.0) | 27 (1.6) |
| Russian Federation | 53 (1.4) | 78 (1.2) | 62 (1.3) | 19 (0.9) | 10 (0.8) |
| Singapore | 61 (1.0) | 97 (0.4) | 75 (0.9) | 15 (1.1) | 60 (1.9) |
| Slovak Republic | 59 (1.9) | 81 (1.0) | 53 (1.6) | 11 (0.8) | 39 (1.9) |
| Slovenia | 60 (1.7) | 76 (1.5) | 57 (1.8) | 19 (0.9) | 28 (1.9) |
| South Africa | 72 (0.8) | 83 (0.7) | 67 (1.2) | 59 (1.4) | 69 (1.1) |
| Thailand | 29 (1.2) | 91 (0.7) | 52 (1.1) | 19 (1.0) | 80 (0.9) |
| Tunisia | 63 (1.2) | 85 (0.9) | 57 (1.0) | 77 (0.7) | 32 (1.1) |
| Turkey | 35 (1.1) | 84 (0.7) | 38 (0.9) | 22 (0.8) | 21 (1.2) |
| United States | 79 (1.2) | 94 (0.6) | 86 (0.7) | 29 (1.3) | 74 (1.6) |
| International Avg. | 55 (0.2) | 86 (0.2) | 59 (0.2) | 36 (0.2) | 42 (0.2) |

Background data provided by students.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates data are not available.
An " $r$ " indicates a $70-84 \%$ student response rate

|  | Percentage of Students Reporting Almost Always or Pretty Often |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Teacher <br> Uses the Board | Teacher Uses an Overhead Projector | Teacher Uses a Computer to Demonstrate Ideas in Mathematics | Students Use the Board | Students Use an Overhead Projector |
| Australia | 96 (0.8) | 10 (1.5) | 4 (0.4) | 15 (1.4) | 3 (0.4) |
| Belgium (Flemish) | 96 (0.7) | 11 (1.7) | 2 (0.5) | 42 (1.8) | 2 (0.8) |
| Bulgaria | 93 (0.6) | 10 (1.1) | 4 (0.6) | 79 (2.1) | 7 (0.7) |
| Canada | 91 (0.9) | 42 (2.7) | 5 (0.5) | 25 (1.2) | 7 (0.8) |
| Chile | 96 (0.6) | 10 (0.8) | 10 (0.9) | 79 (1.5) | 6 (0.6) |
| Chinese Taipei | 96 (0.4) | 4 (0.4) | 2 (0.2) | 48 (1.6) | 2 (0.3) |
| Cyprus | 97 (0.3) | 12 (0.7) | 7 (0.6) | 92 (0.6) | 8 (0.5) |
| Czech Republic | 97 (0.4) | 9 (1.6) | 2 (0.4) | 91 (1.7) | 4 (0.5) |
| England | 94 (1.5) | 19 (2.6) | 6 (0.8) | 13 (1.0) | 3 (0.6) |
| Finland | 94 (1.4) | 42 (2.9) | 2 (0.4) | 52 (2.6) | 5 (0.7) |
| Hong Kong, SAR | 96 (0.4) | 9 (0.8) | 3 (0.4) | 46 (1.7) | 3 (0.4) |
| Hungary | 96 (0.6) | 6 (0.7) | 3 (0.4) | 62 (1.7) | 3 (0.4) |
| Indonesia | 93 (0.5) | 6 (0.5) | 2 (0.5) | 45 (1.4) | 4 (0.4) |
| Iran, Islamic Rep. | 94 (0.5) | 8 (0.6) | 0 (0.1) | 89 (0.7) | 5 (0.4) |
| Israel | 90 (0.6) | 19 (1.1) | 11 (0.9) | 40 (1.6) | 13 (0.9) |
| Italy | 94 (0.5) | 8 (0.9) | 5 (0.6) | 84 (1.1) | 7 (0.6) |
| Japan | 99 (0.2) | 4 (0.8) | 1 (0.4) | 50 (2.5) | 1 (0.3) |
| Jordan | 91 (0.6) | 23 (1.0) | 12 (1.2) | 80 (0.9) | 19 (1.0) |
| Korea, Rep. of | 93 (0.5) | 10 (0.8) | 7 (0.9) | 38 (1.7) | 3 (0.3) |
| Latvia (LSS) | 83 (1.3) | 7 (1.1) | 5 (0.7) | 83 (1.7) | 4 (0.5) |
| Lithuania ${ }^{\ddagger}$ | - - | - - | - - | - - | - - |
| Macedonia, Rep. of | 95 (0.7) | 22 (1.5) | 6 (0.8) | 89 (1.1) | 14 (0.9) |
| Malaysia | 96 (0.5) | 6 (1.0) | 1 (0.2) | 52 (1.4) | 3 (0.3) |
| Moldova | 83 (0.9) | 37 (1.8) | 13 (1.1) | 85 (0.8) | 31 (1.6) |
| Morocco | $r \quad 87$ (0.7) | $5 \quad 32$ (1.1) | s $\quad 9(1.0)$ | 71 (1.2) | s 24 (1.0) |
| Netherlands | 90 (1.6) | 7 (1.4) | 2 (0.3) | 9 (1.2) | 2 (0.3) |
| New Zealand | 95 (0.8) | 32 (2.7) | 7 (0.7) | 24 (1.5) | 7 (0.7) |
| Philippines | 89 (0.7) | 35 (1.4) | 19 (1.5) | 63 (1.1) | 30 (1.4) |
| Romania | 94 (0.4) | 12 (0.9) | 2 (0.3) | 92 (0.7) | 9 (0.8) |
| Russian Federation | 96 (0.4) | 7 (1.0) | 1 (0.2) | 92 (0.6) | 4 (0.5) |
| Singapore | 96 (1.3) | 75 (2.1) | 11 (1.2) | 52 (2.0) | 21 (1.1) |
| Slovak Republic | 89 (1.2) | 10 (1.4) | 2 (0.3) | 95 (0.6) | 3 (0.4) |
| Slovenia | 95 (0.5) | 29 (2.2) | 5 (0.6) | 72 (2.1) | 7 (0.7) |
| South Africa | 86 (0.8) | 45 (1.6) | - - | 56 (1.7) | 36 (1.5) |
| Thailand | 93 (0.8) | 7 (0.8) | 6 (0.6) | 33 (1.5) | 4 (0.5) |
| Tunisia | 84 (0.8) | 13 (0.8) | 1 (0.3) | 71 (0.9) | 8 (0.6) |
| Turkey | 93 (0.4) | 13 (0.8) | 2 (0.3) | 80 (0.9) | 8 (0.6) |
| United States | 80 (1.9) | 59 (3.3) | 9 (0.7) | 37 (1.9) | 16 (1.0) |
| International Avg. | 92 (0.1) | 19 (0.3) | 5 (0.1) | 60 (0.2) | 9 (0.1) |

Background data provided by students.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

A dash (-) indicates data are not available.
An "r" indicates a $70-84 \%$ student response rate. An " $s$ " indicates a 50-69\% student response rate.

Exhibit 6.13 Index of Teachers' Emphasis on Mathematics Reasoning and Problem-Solving (EMRPS)


Index based on teachers' responses to four questions about how often they ask students to: 1) explain the reasoning behind an idea; 2) represent and analyze relationships using tables, charts, or graphs; 3) work on problems for which there is no immediately obvious method of solution; 4) write equations to represent relationships (see reference exhibit R3.9).
Average is computed across the four items based on a 4point scale: $1=$ never or almost never; 2 = some lessons; 3 = most lessons; 4 = every lesson. High level indicates average is greater than or equal to 3 . Medium level indicates average is greater than or equal to 2.25 and less than 3. Low level indicates average is less than 2.25.


[^12][^13]

Exhibit 6.14 Trends in Index of Teachers' Emphasis on Mathematics Reasoning and Problem-Solving (EMRPS)

TIMSS 1999
8
Mathematics

|  | High <br> EMRPS <br> Percent of Students |  |  |  | Medium EMRPS <br> Percent of Students |  |  |  | Low <br> EMRPS <br> Percent of Students |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1995 | 1999 | 1995-1999 Difference |  | 1995 | 1999 | 1995-1999 Difference |  | 1995 | 1999 | 1995-1999 <br> Difference |  |
| Australia | 2 (1.1) | 7 (2.1) | 5 (2.4) | - | 43 (3.8) | 54 (4.5) | 11 (5.9) | - | 55 (3.9) | 39 (4.3) | -16 (5.8) | - |
| Belgium (Flemish) | 0 (0.0) | 1 (0.4) | 1 (0.4) | $\bullet$ | 29 (3.3) | 39 (3.1) | 10 (4.5) | - | 71 (3.3) | 61 (3.1) | -11 (4.5) | - |
| Canada | 4 (1.7) | 13 (2.0) | 9 (2.6) | $\triangle$ | 54 (5.0) | 62 (3.4) | 8 (6.0) | - | 42 (5.1) | 26 (3.0) | -16 (6.0) | - |
| Cyprus | 20 (4.4) | 13 (3.5) | -7 (5.6) | $\bullet$ | 51 (6.0) | 68 (4.9) | 16 (7.7) | - | 29 (5.6) | 19 (3.8) | -9 (6.8) | - |
| Czech Republic | 18 (4.1) | 21 (4.2) | 3 (5.8) | - | 65 (5.9) | 73 (4.6) | 8 (7.5) | - | 17 (5.0) | 6 (2.6) | -11 (5.7) | - |
| England | 4 (1.4) | 3 (1.4) | -1 (2.0) | - | 62 (3.2) | 66 (3.5) | 4 (4.7) | - | 34 (3.1) | 31 (3.4) | -4 (4.6) | - |
| Hong Kong, SAR | 5 (2.4) | 6 (2.2) | 1 (3.2) | - | 41 (5.5) | 56 (3.6) | 15 (6.6) | $\bigcirc$ | 54 (5.4) | 38 (3.7) | -16 (6.5) | - |
| Hungary | 20 (3.1) | 16 (3.0) | -4 (4.3) | $\bigcirc$ | 71 (4.0) | 74 (3.3) | 3 (5.2) | - | 10 (2.4) | 10 (2.3) | 1 (3.4) | - |
| Iran, Islamic Rep. | 6 (2.1) | 16 (3.5) | 10 (4.0) | - | 52 (5.3) | 45 (4.2) | -7 (6.7) | - | 42 (5.4) | 39 (4.1) | -3 (6.8) | - |
| Israel ${ }^{\dagger}$ | 13 (4.5) | 17 (2.8) | 4 (5.3) | - | 58 (7.5) | 62 (3.6) | 4 (8.3) | - | 29 (7.6) | 21 (3.1) | -8 (8.2) | - |
| Italy | 15 (3.4) | 28 (3.8) | 14 (5.1) | - | 66 (4.7) | 58 (4.5) | -8 (6.5) | - | 19 (3.5) | 14 (3.3) | -6 (4.8) | - |
| Japan | 37 (4.1) | 49 (4.1) | 12 (5.9) | - | 54 (4.1) | 45 (4.1) | -9 (5.8) | - | 10 (2.3) | 7 (2.1) | -3 (3.1) | - |
| Korea, Rep. of | 15 (3.2) | 21 (3.0) | 6 (4.4) | $\bullet$ | 70 (4.2) | 66 (3.3) | -4 (5.3) | $\bigcirc$ | 15 (3.5) | 13 (2.4) | -2 (4.3) | - |
| Latvia (LSS) | 14 (3.8) | 6 (2.0) | -8 (4.2) | - | 60 (4.9) | 64 (4.4) | 4 (6.6) | $\bigcirc$ | 26 (4.2) | 30 (4.1) | 4 (5.9) | - |
| Lithuania | 6 (2.1) | 9 (2.4) | 4 (3.2) | - | 66 (3.9) | 67 (3.7) | 1 (5.4) | - | 28 (3.9) | 23 (3.7) | -5 (5.4) | - |
| Netherlands | -- | -- | -- |  |  |  | -- |  | -- | - - | - - |  |
| New Zealand s | 2 (1.2) | 5 (2.2) | 3 (2.5) | $\bullet$ | 50 (4.1) | 48 (4.3) | -2 (6.0) | - | 49 (4.3) | 47 (4.0) | -2 (5.9) | - |
| Romania | 26 (3.6) | 22 (4.5) | -3 (5.8) | - | 69 (4.0) | 73 (4.4) | 5 (5.9) | $\bigcirc$ | 6 (1.9) | 4 (1.7) | -1 (2.5) | - |
| Russian Federation | 5 (1.6) | 11 (2.5) | 6 (3.0) | - | 78 (4.0) | 74 (3.9) | -4 (5.6) | - | 17 (3.6) | 15 (3.6) | -2 (5.0) | - |
| Singapore s | 2 (1.4) | 7 (2.1) | 5 (2.5) | - | 48 (4.9) | 47 (4.0) | -1 (6.3) | - | 50 (4.8) | 47 (4.4) | -3 (6.5) | - |
| Slovak Republic | 12 (2.7) | 18 (3.9) | 6 (4.7) | - | 80 (3.1) | 71 (4.2) | -8 (5.3) | - | 8 (2.2) | 10 (2.8) | 2 (3.6) | - |
| Slovenia | 11 (2.9) | 21 (3.6) | 10 (4.6) | $\bullet$ | 74 (4.3) | 72 (3.9) | -3 (5.9) | - | 14 (3.6) | 7 (2.0) | -8 (4.1) | - |
| Thailand ${ }^{\dagger}$ | 2 (0.3) | 6 (1.6) | 4 (1.6) | $\bullet$ | 36 (5.4) | 58 (4.7) | 21 (7.1) | - | 62 (5.5) | 36 (4.5) | -25 (7.1) | $\nabla$ |
| United States | 10 (2.7) | 18 (2.5) | 8 (3.7) | $\bullet$ | 52 (3.7) | 57 (2.9) | 5 (4.7) | - | 38 (3.6) | 24 (2.7) | -13 (4.5) | - |
| International Avg. § | 11 (0.6) | 15 (0.6) | 4 (0.9) | $\Delta$ | 59 (1.0) | 61 (0.9) | 2 (1.3) | - | 30 (0.9) | 24 (0.7) | -6 (1.1) | $\nabla$ |

A 1999 significantly higher than 1995

- No significant difference between 1995 and 1999
v 1999 significantly lower than 1995

Significance tests adjusted for multiple comparisons

Background data provided by teachers.
$\dagger$ Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates data are not available.
An " $s$ " indicates teacher response data available for $50-69 \%$ of students, based on the lower response rate in either 1995 or 1999.

## How Are Calculators and Computers Used?

Exhibit 6.15 shows data on students' access to calculators for use in mathematics class and policies on their use for those with access. In 14 countries, teachers reported that nearly all students (more than go percent) had access to calculators in class. The countries with this high degree of access were Australia, Belgium (Flemish), Canada, the Czech Republic, England, Finland, Hong Kong, Israel, Lithuania, the Netherlands, New Zealand, Singapore, the Slovak Republic, and the United States. For students in classes with access to calculators, most teachers reported some type of restricted use (for about two-thirds of the students on average internationally).

TIMss combined students' and teachers' reports on the frequency of calculator use to create an index of emphasis on calculators in mathematics class (ECMC), presented in Exhibit 6.16. Students were placed in the high category if they reported using calculators in class almost always or pretty often and their teachers reported calculator use of at least once or twice a week. At the other end of the spectrum, students were placed at the low level if they reported using calculators only once in a while or never and their teachers reported asking students to use calculators never or hardly ever. There was enormous variation in the results across countries. The Netherlands, Singapore, and Australia had more than four-fifths of their students (from 84 percent to 95 percent) in the high category. In contrast, a number of countries had half or more of their students in the low category, including Chinese Taipei, Iran, Korea, Japan, Malaysia, Romania, Thailand, and Turkey. Since several high-performing countries have restricted calculator use and large percentages of students are in the low-use category, the relationship between calculator use and performance is difficult to interpret. Although on average internationally the relationship is unclear, in most of the countries where emphasis on calculator use was high, there was a positive association between calculator use and mathematics achievement.

Exhibit R9. 12 in the reference section shows the detailed results for students' reports on frequency of calculator use. In the Netherlands, 67 percent of the students reported almost always using calculators in their mathematics lessons. Countries with the next highest level of use included Canada, Israel, New Zealand, South Africa, and the United States (from 42 to 45 percent). Exhibit R3. 13 shows the trends between 1995 and 1999. Internationally on average, there was a small but significant decrease in the percentage of students who reported that they almost always used calculators. Teachers were asked how often they asked stu-

dents to use calculators for a variety of activities. The percentages of students asked to use calculators for each activity at least once or twice a week are shown in Exhibit R3.14. According to teachers, they asked the most students to use calculators at least weekly for checking answers, performing routine computations, and solving complex problems (43 to 44 percent internationally each). About one-fourth of the students across countries were asked to explore number concepts and one-fifth to use calculators on their tests.

Exhibit 6.17 shows trend data for the index of emphasis on calculators in mathematics class. There was a shift toward less frequent use of calculators between 1995 and 1999. Significantly fewer students were at the high level of the emphasis on calculators index in 1999 than in 1995 in five countries: the Czech Republic, England, Latvia (Lss), the Russian Federation, and the Slovak Republic. Two countries, Belgium (Flemish) and Thailand, had increased percentages of students in the high category. As shown in Exhibit R3.13, changes in students' reports on the frequency of calculator use from 1995 to 1999 show a significant decrease in the percentage of students in the almost always category in eight countries: Cyprus, the Czech Republic, England, Hong Kong, Latvia, Romania, the Russian Federation, and the Slovak Republic. The Netherlands and Singapore, however, showed increases in that category.

Students' reports on their frequency of computer use in mathematics class are presented in Exhibit 6.18. Across countries, the vast majority of students ( 80 percent on average internationally) reported never using computers in mathematics class. The trend data, however, show a small but statistically significant shift from the never to the once in a while category (see Exhibit 6.19). Significantly more students reported using computers in mathematics class once in a while in 1999 than in 1995 in six countries: Canada, Hong Kong, Korea, Singapore, Slovenia, and Thailand.

Because the Internet provides a wealth of opportunities for students to collect and analyze data, timss began asking about students' access to the Internet and whether they used the World Wide Web to access information for mathematics projects. The data in Exhibit 6.20 indicate great variation across countries in Internet access. Still, the international averages show about one-quarter of the students with access to the Internet at school. The international average for using the Internet to access information for mathematics class on even a monthly basis was 10 percent (less than half those reporting access).


[^14]Exhibit 6.16 Index of Emphasis on Calculators in Mathematics Class (ECMC)*

| Index of Emphasis on Calculators in Mathematics Class |  | High ECMC |  | Medium ECMC |  | Low ECMC |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Index based on students' reports of the frequency of using calculators in mathematics lessons and teachers' reports of students' | Netherlands Singapore Australia England Canada | 95 (1.1) <br> 85 (1.6) <br> 84 (2.4) <br> 80 (2.3) <br> 79 (1.9) | $\begin{aligned} & 538(7.2) \\ & 611(6.3) \\ & 531(5.5) \\ & 524(5.7) \\ & 537(3.0) \end{aligned}$ | $\begin{array}{r} 5(1.1) \\ 15(1.6) \\ 12(1.8) \\ 19(2.2) \\ 18(1.7) \end{array}$ | $\begin{aligned} & 512 \text { (23.5) } \\ & 567 \text { (7.1) } \\ & 515 \text { (12.9) } \\ & 462 \text { (6.5) } \\ & 523 \text { (4.7) } \end{aligned}$ | $\begin{aligned} & 0(0.0) \\ & 0(0.0) \\ & 4(1.6) \\ & 1(0.7) \\ & 3(0.9) \end{aligned}$ | $484 \text { (24.7) }$ $548 \text { (6.8) }$ |
| use of calculators in mathematics class for five activities: checking answers; tests and exams; routine computation; solving complex problems; and exploring | New Zealand Hong Kong, SAR <br> Israel <br> United States <br> Italy | $\begin{array}{ll} 77 & (2.8) \\ 75 & (1.9) \\ 67 & (2.4) \\ 65 & (3.2) \\ 52 & (2.4) \end{array}$ | 494 (5.5) <br> 586 (4.4) <br> 472 (4.3) <br> 515 (4.5) <br> 486 (4.6) | $\begin{array}{ll} 19 & (2.2) \\ 25 & (1.8) \\ 31 & (2.3) \\ 31 & (2.9) \\ 37 & (2.3) \end{array}$ | 482 (9.9) <br> 577 (6.3) <br> 468 (8.4) <br> 489 (6.4) <br> 474 (5.7) | $\begin{array}{r} 4(1.7) \\ 0(0.2) \\ 2(0.7) \\ 5(1.2) \\ 11(1.8) \end{array}$ | $\begin{gathered} 537(28.2) \\ \sim \sim \\ \sim \sim \\ 476(10.8) \\ 483(12.0) \end{gathered}$ |
| number concepts (see reference exhibits R3.12R3.14). High level indicates the student reported using calculators in mathematics lessons almost always or pretty | South Africa Finland Slovak Republic Belgium (Flemish) Czech Republic | 51 (2.8) <br> 46 (3.0) <br> 41 (3.1) <br> 39 (2.7) <br> 35 (3.2) | 280 (9.9) <br> 520 (3.5) <br> 541 (5.8) <br> 571 (6.3) <br> 528 (7.1) | 40 (1.9) <br> 47 (2.9) <br> 55 (3.3) <br> 54 (2.7) <br> 60 (3.5) | $\begin{aligned} & 266(7.3) \\ & 523(3.4) \\ & 527(4.4) \\ & 562 \text { (6.9) } \\ & 517 \text { (4.7) } \end{aligned}$ | $\begin{array}{r} 10(2.0) \\ 6(1.9) \\ 3(1.7) \\ 7(2.6) \\ 5(2.0) \end{array}$ | $\begin{aligned} & 314 \text { (24.3) } \\ & 517 \text { (8.6) } \\ & 521 \text { (18.3) } \\ & 532 \text { (27.9) } \\ & 507 \text { (26.2) } \end{aligned}$ |
| often, and the teacher reported students use calculators at least once or twice a week for any of the tasks. Low level indicates the student reported using | Russian Federation <br> Hungary <br> Moldova <br> Morocco s <br> Chile | $\begin{array}{ll} 29 & (2.3) \\ 28 & (2.4) \\ 24 & (1.6) \\ 18 & (1.3) \\ 18 & (1.9) \end{array}$ | $\begin{aligned} & 522(9.3) \\ & 535(6.3) \\ & 476(5.4) \\ & 321(4.6) \\ & 404(8.9) \end{aligned}$ | $\begin{aligned} & 60(2.1) \\ & 53(3.1) \\ & 59(2.1) \\ & 59(1.7) \\ & 55(2.8) \end{aligned}$ | $\begin{aligned} & 528(6.3) \\ & 530(5.1) \\ & 468(5.0) \\ & 343(3.6) \\ & 395(5.2) \end{aligned}$ | $\begin{aligned} & 12(2.4) \\ & 19(2.8) \\ & 17(2.6) \\ & 22(1.9) \\ & 27(2.9) \end{aligned}$ | $\begin{aligned} & 539 \text { (13.3) } \\ & 527 \text { (8.6) } \\ & 467 \text { (10.2) } \\ & 350 \text { (6.8) } \\ & 389(7.3) \end{aligned}$ |
| calculators once in a while or never, and the teacher reported students use calculators never or hardly ever for all of the tasks. Medium level includes all other possible | Latvia (LSS) Cyprus <br> Macedonia, Rep. of Jordan Slovenia | 16 (2.2) <br> 14 (1.8) <br> 14 (1.8) <br> 10 (1.4) <br> 10 (1.6) | $\begin{aligned} & 514(8.6) \\ & 468(5.6) \\ & 465(8.6) \\ & 416(10.8) \\ & 518(8.6) \end{aligned}$ | 53 (3.6) <br> 56 (3.3) <br> 47 (2.6) <br> 62 (3.1) <br> 62 (3.4) | $\begin{aligned} & 502(4.8) \\ & 477(3.2) \\ & 455(5.2) \\ & 431(5.0) \\ & 530(3.8) \end{aligned}$ | 31 (3.4) <br> 30 (3.9) <br> 39 (3.5) <br> 28 (3.5) <br> 29 (3.9) | 505 (4.4) <br> 483 (4.3) <br> 448 (6.7) <br> 446 (6.7) <br> 538 (4.3) |
| combinations of responses. | Bulgaria Philippines Indonesia Tunisia Romania | $\begin{aligned} & 8(1.2) \\ & 6(1.1) \\ & 6(1.0) \\ & 4(0.7) \\ & 3(0.7) \end{aligned}$ | $\begin{aligned} & 501 \text { (14.0) } \\ & 321 \text { (16.1) } \\ & 415 \text { (13.7) } \\ & 424 \text { (8.2) } \\ & 477 \text { (17.5) } \end{aligned}$ | 68 (3.5) <br> 48 (2.9) <br> 60 (4.1) <br> 60 (3.5) <br> 39 (3.8) | 518 (4.9) <br> 342 (7.2) <br> 411 (7.0) <br> 444 (2.7) <br> 487 (9.3) | 24 (3.9) <br> 46 (3.4) <br> 34 (4.3) <br> 35 (3.6) <br> 58 (4.1) | $\begin{array}{ll} 503(19.4) \\ 352(8.1) \\ 391 & (9.2) \\ 456(4.4) \\ 470 & (5.6) \end{array}$ |
|  | Turkey | 3 (0.4) | 411 (11.5) | 42 (4.0) | 428 (4.9) | 55 (4.2) | 433 (5.6) |
|  | Iran, Islamic Rep. | 2 (0.5) | ~ ~ | 42 (3.9) | 425 (5.5) | 56 (4.2) | 422 (4.0) |
|  | Thailand | 2 (0.3) | ~ ~ | 39 (3.4) | 478 (7.8) | 59 (3.6) | 459 (6.2) |
|  | Chinese Taipei | 2 (0.4) | ~ ~ | 48 (4.0) | 576 (4.8) | 50 (4.2) | 598 (5.4) |
|  |  | 1 (0.3) | ~ ~ | 35 (4.1) | 522 (8.8) | 64 (4.2) | 518 (6.1) |
|  | Korea, Rep. of | 0 (0.3) | $\sim$ | 29 (3.3) | 587 (4.0) | 71 (3.3) | 587 (2.4) |
|  | Japan | 0 (0.1) | ~ ~ | 21 (3.2) | 573 (6.4) | 79 (3.2) | 579 (2.2) |
|  | Lithuania ${ }^{\text { }}$ | -- | - | -- | - - | -- | -- |
|  | International Avg. | 32 (0.3) | 481 (1.8) | 42 (0.5) | 484 (1.2) | 26 (0.5) | 481 (3.3) |

* The use of calculators on TIMSS was not allowed in 1995 or in 1999.
$\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^15]

Exhibit 6.17 Trends in Index of Emphasis on Calculators in Mathematics Class (ECMC)*
TIMSS 1999
8
Mathematics

|  | HighECMCPercent of Students |  |  |  | Medium <br> ECMC <br> Percent of Students |  |  |  | Low <br> ECMC <br> Percent of Students |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1995 | 1999 | 1995-1999 <br> Differenc |  | 1995 | 1999 | 1995-1999 <br> Difference |  | 1995 | 1999 | 1995-1999 <br> Difference |  |
| Australia | 85 (2.5) | 84 (2.4) | -1 (3.5) | - | 11 (1.6) | 12 (1.8) | 1 (2.4) | - | 4 (1.5) | 4 (1.6) | 0 (2.2) | - |
| Belgium (Flemish) | 20 (3.2) | 39 (2.7) | 19 (4.2) | $\triangle$ | 43 (3.9) | 54 (2.7) | 11 (4.8) | - | 37 (4.7) | 7 (2.6) | -30 (5.4) | $\checkmark$ |
| Canada | 70 (2.6) | 79 (1.9) | 9 (3.3) | - | 26 (2.1) | 18 (1.7) | -7 (2.6) | - | 5 (2.6) | 3 (0.9) | -2 (2.7) | - |
| Cyprus | 23 (3.7) | 14 (1.8) | -9 (4.1) | - | 56 (3.9) | 56 (3.3) | -1 (5.1) | - | 21 (4.8) | 30 (3.9) | 9 (6.2) | - |
| Czech Republic | 59 (3.8) | 35 (3.2) | -24 (5.0) | $\nabla$ | 38 (3.7) | 60 (3.5) | 23 (5.1) | $\triangle$ | 3 (1.8) | 5 (2.0) | 1 (2.7) | - |
| England | 90 (1.3) | 80 (2.3) | -10 (2.7) | $\nabla$ | 10 (1.3) | 19 (2.2) | 9 (2.6) | $\triangle$ | 0 (0.0) | 1 (0.7) | 1 (0.7) | - |
| Hong Kong, SAR | 76 (4.2) | 75 (1.9) | -1 (4.6) | - | 18 (3.5) | 25 (1.8) | 7 (3.9) | $\bullet$ | 6 (2.4) | 0 (0.2) | -5 (2.4) | - |
| Hungary | 37 (3.2) | 28 (2.4) | -8 (4.0) | - | 44 (2.8) | 53 (3.1) | 9 (4.2) | - | 20 (3.5) | 19 (2.8) | -1 (4.5) | - |
| Iran, Islamic Rep. r | 1 (0.4) | 2 (0.5) | 1 (0.6) | - | 49 (4.7) | 42 (3.9) | -7 (6.1) | $\bullet$ | 50 (4.7) | 56 (4.2) | 6 (6.4) | - |
| Israel ${ }^{\dagger}$ | 63 (5.7) | 69 (2.8) | 6 (6.3) | - | 32 (5.1) | 30 (2.7) | -3 (5.8) | $\bullet$ | 5 (2.8) | 1 (0.8) | -4 (2.9) | - |
| Italy | 48 (3.9) | 53 (3.1) | 5 (5.0) | - | 42 (3.6) | 38 (2.8) | -5 (4.6) | $\bullet$ | 10 (2.4) | 10 (2.1) | 0 (3.2) | - |
| Japan | 0 (0.2) | 0 (0.1) | 0 (0.2) | - | 23 (3.2) | 21 (3.2) | -3 (4.5) | $\bullet$ | 76 (3.3) | 79 (3.2) | 3 (4.6) | - |
| Korea, Rep. of | 0 (0.1) | 0 (0.3) | 0 (0.3) | - | 25 (3.7) | 29 (3.3) | 3 (4.9) | - | 74 (3.7) | 71 (3.3) | -3 (5.0) | - |
| Latvia (LSS) | 49 (3.7) | 16 (2.2) | -33 (4.4) | $\checkmark$ | 42 (3.0) | 53 (3.6) | 11 (4.7) | $\bullet$ | 9 (2.5) | 31 (3.4) | 22 (4.2) | $\Delta$ |
| Lithuania | - - | - - |  |  |  |  | - - |  | - - | - - | - - |  |
| Netherlands | 89 (2.2) | 95 (1.1) | 6 (2.4) | $\bullet$ | 11 (2.2) | 5 (1.1) | -6 (2.4) | - | 0 (0.0) | 0 (0.0) | - - | - |
| New Zealand | 70 (2.8) | 77 (2.8) | 7 (3.9) | - | 23 (2.5) | 19 (2.2) | -4 (3.3) | - | 6 (1.9) | 4 (1.7) | -2 (2.6) | - |
| Romania | 5 (1.1) | 3 (0.7) | -2 (1.3) | - | 42 (3.3) | 39 (3.8) | -3 (5.0) | - | 54 (3.7) | 58 (4.1) | 5 (5.5) | - |
| Russian Federation | 50 (3.0) | 29 (2.3) | -21 (3.8) | $\nabla$ | 44 (2.8) | 60 (2.1) | 16 (3.5) | $\triangle$ | 7 (1.8) | 12 (2.4) | 5 (3.0) | - |
| Singapore | 79 (2.2) | 85 (1.6) | 6 (2.7) | - | 20 (2.1) | 15 (1.6) | -5 (2.6) | - | 1 (0.1) | 0 (0.0) | -1 (0.1) | $\checkmark$ |
| Slovak Republic | 68 (2.8) | 41 (3.1) | -26 (4.2) | $\nabla$ | 32 (2.8) | 55 (3.3) | 24 (4.3) | $\triangle$ | 1 (0.6) | 3 (1.7) | 3 (1.8) | - |
| Slovenia | 13 (2.1) | 10 (1.6) | -3 (2.6) | - | 55 (3.8) | 62 (3.4) | 7 (5.1) | $\bigcirc$ | 32 (4.4) | 29 (3.9) | -4 (5.8) | - |
| Thailand ${ }^{+}$r | 1 (0.2) | 2 (0.3) | 1 (0.4) | $\triangle$ | 33 (5.2) | 39 (3.4) | 6 (6.2) | - | 66 (5.2) | 59 (3.6) | -7 (6.3) | - |
| United States | 67 (3.4) | 65 (3.2) | -2 (4.7) | - | 27 (2.5) | 31 (2.9) | 4 (3.8) | $\bullet$ | 7 (1.9) | 5 (1.2) | -2 (2.2) | - |
| International Avg. § | 47 (0.6) | 43 (0.5) | -4 (0.8) | $\nabla$ | 33 (0.7) | 36 (0.6) | 3 (0.9) | $\triangle$ | 20 (0.6) | 20 (0.6) | 1 (0.8) | - |



Background data provided by students and teachers.

* The use of calculators on TIMSS was not allowed in 1995 or in 1999
† Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
An " $r$ " indicates teacher and/or student response data available for $70-84 \%$ of students.

|  | Almost Always or Pretty Often |  | Once in a While |  | Never |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Australia | 6 (1.1) | 502 (15.1) | 23 (2.3) | 535 (6.0) | 71 (3.0) | 524 (5.7) |
| Belgium (Flemish) | 1 (0.4) | ~ ~ | 5 (1.2) | 536 (17.4) | 93 (1.3) | 562 (3.1) |
| Bulgaria | 3 (0.5) | 473 (15.4) | 4 (0.5) | 486 (12.3) | 93 (0.8) | 517 (5.9) |
| Canada | 8 (0.7) | 507 (7.1) | 25 (1.5) | 534 (3.8) | 67 (1.6) | 534 (2.5) |
| Chile | 8 (0.9) | 362 (12.1) | 11 (0.9) | 388 (7.7) | 81 (1.6) | 399 (4.5) |
| Chinese Taipei | 13 (0.6) | 548 (7.5) | 21 (0.6) | 564 (5.2) | 66 (0.9) | 601 (3.8) |
| Cyprus | 6 (0.4) | 422 (6.0) | 13 (0.7) | 459 (5.3) | 81 (0.8) | 485 (2.2) |
| Czech Republic | 2 (0.7) | ~ | 14 (2.4) | 526 (8.4) | 84 (2.6) | 520 (3.8) |
| England | 11 (1.7) | 466 (10.4) | 43 (2.2) | 512 (5.1) | 46 (2.7) | 492 (5.2) |
| Finland | 3 (0.9) | 487 (10.8) | 21 (2.2) | 524 (4.4) | 76 (2.7) | 521 (3.1) |
| Hong Kong, SAR | 8 (0.5) | 561 (9.5) | 18 (0.8) | 577 (6.2) | 75 (1.1) | 587 (4.1) |
| Hungary | 3 (0.5) | 481 (18.9) | 6 (1.0) | 501 (11.3) | 92 (1.2) | 536 (3.6) |
| Indonesia | 1 (0.3) | ~ ~ | 4 (0.4) | 389 (16.2) | 95 (0.5) | 407 (4.6) |
| Iran, Islamic Rep. | 0 (0.2) | ~ ~ | 4 (0.4) | 413 (10.7) | 96 (0.4) | 426 (3.3) |
| Israel | 14 (1.0) | 429 (9.3) | 19 (1.5) | 470 (8.2) | 67 (2.2) | 479 (4.2) |
| Italy | 11 (1.3) | 464 (7.4) | 17 (1.6) | 489 (5.5) | 72 (2.3) | 482 (4.0) |
| Japan | 2 (0.5) | $\sim \sim$ | 21 (2.3) | 576 (3.7) | 76 (2.7) | 581 (2.0) |
| Jordan r | 13 (1.2) | 377 (5.9) | 12 (0.8) | 406 (7.3) | 75 (1.6) | 454 (4.2) |
| Korea, Rep. of | 3 (0.3) | 567 (7.9) | 13 (0.7) | 596 (3.9) | 83 (0.8) | 587 (2.2) |
| Latvia (LSS) | 2 (0.3) | ~ ~ | 3 (0.6) | 475 (15.3) | 95 (0.6) | 507 (3.4) |
| Lithuania ${ }^{\ddagger}$ |  |  |  |  |  | -- |
| Macedonia, Rep. of | 4 (0.6) | 395 (12.8) | 8 (0.5) | 420 (8.8) | 88 (0.8) | 462 (3.7) |
| Malaysia | 1 (0.2) | ~ ~ | 6 (0.4) | 524 (8.2) | 93 (0.4) | 520 (4.3) |
| Moldova | 11 (0.9) | 434 (7.3) | 16 (1.2) | 461 (5.9) | 73 (1.7) | 480 (4.4) |
| Morocco s | 6 (0.8) | 313 (15.8) | 10 (0.8) | 336 (11.9) | 84 (1.2) | 350 (4.0) |
| Netherlands | 1 (0.2) | ~ ~ | 19 (3.2) | 543 (9.6) | 80 (3.2) | 541 (8.2) |
| New Zealand | 6 (0.7) | 426 (9.4) | 21 (2.2) | 517 (8.8) | 73 (2.4) | 491 (5.5) |
| Philippines | 8 (1.0) | 294 (9.5) | 12 (0.7) | 319 (11.3) | 80 (1.3) | 362 (5.8) |
| Romania | 1 (0.3) | ~ ~ | 5 (0.4) | 447 (13.0) | 93 (0.5) | 481 (5.4) |
| Russian Federation | 1 (0.2) | ~ | 3 (0.4) | 513 (11.1) | 97 (0.4) | 530 (5.7) |
| Singapore | 11 (0.8) | 590 (11.0) | 43 (2.5) | 625 (6.8) | 46 (2.7) | 589 (6.1) |
| Slovak Republic | 1 (0.2) | ~ ~ | 4 (0.9) | 536 (10.2) | 95 (1.0) | 535 (3.9) |
| Slovenia | 5 (0.6) | 473 (9.9) | 15 (1.2) | 516 (6.5) | 81 (1.4) | 537 (2.5) |
| South Africa | -- | -- | -- | -- | -- | -- |
| Thailand | 5 (0.6) | 431 (12.8) | 10 (0.6) | 471 (7.4) | 85 (1.0) | 470 (5.0) |
| Tunisia | 1 (0.2) | ~ ~ | 9 (0.5) | 440 (5.3) | 90 (0.6) | 451 (2.4) |
| Turkey | 2 (0.2) | ~ ~ | 5 (0.5) | 415 (11.2) | 93 (0.6) | 436 (4.3) |
| United States | 12 (1.1) | 463 (7.3) | 27 (2.0) | 520 (5.2) | 61 (2.7) | 506 (4.0) |
| International Avg. | 5 (0.1) | 455 (2.8) | 14 (0.2) | 488 (1.5) | 80 (0.3) | 498 (0.7) |

[^16]A dash (-) indicates data are not available. A tilde ( ) indicates insufficient data to report achievement.
An " $r$ " indicates a $70-84 \%$ student response rate. An "s" indicates a $50-69 \%$ student response rate.

|  | Almost Always or Pretty Often |  |  | Once in a While |  |  | Never |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Percent of Students 1999 | 1995-1999 <br> Difference |  | Percent of Students 1999 | 1995-1999 <br> Difference |  | Percent of Students 1999 | 1995-1999 <br> Difference |  |
| Australia | 6 (1.1) | 1 (1.4) | - | 23 (2.3) | 5 (2.9) | - | 71 (3.0) | -6 (3.6) | 。 |
| Belgium (Flemish) r | 1 (0.4) | 0 (0.8) | - | 5 (1.2) | 1 (1.5) | - | 93 (1.3) | -1 (1.7) | - |
| Canada | 8 (0.7) | 4 (0.8) | - | 25 (1.5) | 12 (1.9) | $\triangle$ | 67 (1.6) | -15 (2.2) | $\nabla$ |
| Cyprus | 6 (0.4) | -5 (0.9) | $\checkmark$ | 13 (0.7) | -3 (1.1) | $\bigcirc$ | 81 (0.8) | 8 (1.2) | $\triangle$ |
| Czech Republic s | 2 (0.7) | -2 (1.9) | - | 14 (2.4) | 6 (3.1) | $\bullet$ | 84 (2.6) | -5 (3.9) | - |
| England | 11 (1.7) | 2 (2.0) | - | 43 (2.2) | -3 (3.2) | - | 46 (2.7) | 2 (3.8) | - - |
| Hong Kong, SAR | 8 (0.5) | 4 (0.7) | - | 18 (0.8) | 11 (0.9) | - | 75 (1.1) | -16 (1.3) | - ${ }^{\circ}$ |
| Hungary | 3 (0.5) | 0 (0.6) | - | 6 (1.0) | 0 (1.3) | $\bullet$ | 92 (1.2) | -1 (1.4) | - ${ }_{\circ}^{\circ}$ |
| Iran, Islamic Rep. r | 1 (0.3) | -4 (0.6) | V | 4 (0.3) | 0 (0.5) | - | 96 (0.5) | 3 (1.0) | - |
| Israel ${ }^{\dagger}$ | 11 (1.0) | 0 (3.1) | - | 19 (1.7) | 6 (3.1) | - | 70 (2.4) | -6 (5.1) | $\sum$ |
| Italy | 11 (1.6) | 1 (1.9) | - | 15 (1.6) | 1 (2.2) | - | 74 (2.2) | -2 (3.1) | > |
| Japan s | 2 (0.5) | -2 (1.3) | - | 21 (2.3) | 2 (3.5) | - | 76 (2.7) | 0 (4.2) | - 出 |
| Korea, Rep. of | 3 (0.3) | 2 (0.4) | - | 13 (0.7) | 8 (0.8) | - | 83 (0.8) | -10 (1.0) | - |
| Latvia (LSS) s | 2 (0.3) | -2 (0.5) | $\checkmark$ | 3 (0.6) | -2 (1.1) | $\bullet$ | 95 (0.6) | 4 (1.3) | $\sim$ |
| Lithuania | - - | - - |  | - - | - - |  | - - | - - | $\stackrel{C}{0}$ |
| Netherlands | 1 (0.2) | -1 (0.4) | $\bullet$ | 19 (3.2) | 1 (4.6) | - | 80 (3.2) | -1 (4.7) | - |
| New Zealand | 6 (0.7) | 2 (0.9) | - | 21 (2.2) | 4 (3.1) | - | 73 (2.4) | -5 (3.5) | - |
| Romania | 1 (0.3) | -12 (0.9) | $\nabla$ | 5 (0.4) | -3 (0.8) | $\nabla$ | 93 (0.5) | 15 (1.3) | - $\sum^{\text {N }}$ |
| Russian Federation r | 1 (0.2) | -1 (0.4) | $\nabla$ | 3 (0.4) | -2 (0.7) | $\bullet$ | 97 (0.4) | 3 (0.9) | $\triangle$ |
| Singapore | 11 (0.8) | 9 (1.0) | - | 43 (2.5) | 35 (2.8) | $\triangle$ | 46 (2.7) | -44 (3.1) | , |
| Slovak Republic r | 1 (0.2) | 0 (0.3) | - | 4 (0.9) | -1 (1.3) | $\bullet$ | 95 (1.0) | 1 (1.4) | $\stackrel{\text { E }}{ }$ |
| Slovenia | 5 (0.6) | 1 (0.7) | - | 15 (1.2) | 7 (1.3) | - | 81 (1.4) | -9 (1.6) | - 믈 |
| Thailand ${ }^{\dagger}$ | 5 (0.6) | 2 (0.8) | - | 10 (0.6) | 5 (0.9) | $\triangle$ | 85 (1.0) | -6 (1.4) | - |
| United States | 12 (1.1) | 1 (1.8) | - | 27 (2.0) | 6 (2.7) | - | 61 (2.7) | -8 (3.7) | - |
| International Avg. § | 5 (0.2) | 0 (0.2) | - | 16 (0.4) | 4 (0.5) | $\triangle$ | 79 (0.4) | -4 (0.6) | - |

A 1999 significantly higher than 1995

- No significant difference between 1995 and 1999
v 1999 significantly lower than 1995

Significance tests adjusted for multiple comparisons

Background data provided by students.
$\dagger$ Countries with unapproved sampling procedures at the classroom level in 1995
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for Latvian Speaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
A dash ( - ) indicates data are not available.
An " $r$ " indicates a $70-84 \%$ student response rate, based on the lower response rate in either 1995 or 1999. An " $s$ " indicates a $50-69 \%$ student response rate, based on the lower response rate in either 1995 or 1999.
$\square$
$\square$


[^17]
## What Are the Roles of Homework and Assessment?

The amount of time students spend on homework assignments is an important consideration in examining their opportunity to learn mathe-


R3. 15
. matics. Exhibit 6.21 presents the index of teachers' emphasis on mathematics homework (емн). Students in the high category had teachers who reported giving relatively long homework assignments (more than 30 minutes) on a relatively frequent basis (at least once or twice a week). Those in the low category had teachers who gave short assignments (less than 30 minutes) relatively infrequently (less than once a week or never). The medium level includes all other possible combinations of responses. The detailed results from teachers' reports about the length and frequency of their homework assignments are found in the reference section in Exhibit R9. 15 .

The results show substantial variation across countries in the emphasis placed on homework. More than 70 percent of the students in Iran, Italy, Romania, Thailand, and Malaysia were in the high category. For the majority of countries, most students were in the medium category. Very few students were in the low category. One notable exception is Japan (34 percent in the low category), where students were more likely to spend extra time in tutoring and special schools than doing homework. ${ }^{3}$ There was little relationship between amount of homework assigned and students' performance. Again, lower-performing students may need more homework assignments for remedial reasons. The comparison between 1995 and 1999 data in Exhibit 6.22 shows little change in teachers' reports on the emphasis given to mathematics homework.

Since problem-solving activities will potentially be more beneficial if they can be extended to out-of-class-situations and stretched over a longer time, timss asked teachers how often they assigned homework based on projects and investigations. The data in Exhibit R3. 16 in the reference section show that most students ( 82 percent on average internationally) had teachers that never or rarely give such homework.

One theme in recommendations for educational reform is to make assessment a continuous process that relies on a variety of sources of data and methods, rather than a few high-stakes tests. Exhibit 6.23 shows teachers' reports about the weight given to various types of assessment, which varied greatly from country to country. Internationally, the least weight reportedly was given to external standardized tests, teacher-made objective tests, and projects or practical exercises. On average across countries, about two-fifths of the students (from 37 to 42 percent) had mathematics teachers who reported giving quite a lot or a great deal of weight to such

[^18]assessments. The most heavily weighted assessment was students' responses in class. On average internationally, this was given quite a lot or a great deal of weight for 77 percent of the students. Teachers reported that the next heaviest weight was given to teacher-made tests requiring explanations ( 67 percent of students on average internationally) and to observations of students ( 64 percent).

As shown in Exhibit R3. 17 in the reference section, eighth-grade students reported substantial variation in the frequency of testing in mathematics class. On average internationally, students were split about in half, with 57 percent reporting having a quiz or test in class almost always or pretty often and 43 percent reporting such testing only once in a while or never. At least three-fourths of the students reported frequent testing in Belgium (Flemish), Canada, Chile, Cyprus, the Russian Federation, Tunisia, and the United States. In contrast, at least threefourths of the students reported infrequent testing in Hungary, Korea, Latvia (LSs), and Turkey. There was a tendency for the most frequent testing to be associated with lower-achieving students. One could argue that these students can least afford time diverted from their instructional program. However, teachers may provide shorter lessons and followup quizzes for lower-achieving students to monitor their grasp of the subject matter more closely.

Exhibit 6.21 Index of Teachers' Emphasis on Mathematics Homework (EMH)

| Index of Teachers' <br> Emphasis on <br> Mathematics <br> Homework |  | High <br> EMH |  | Medium EMH |  | Low <br> EMH |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Percent of Students | Average Achievement | Percent of Students | Average Achievement | Percent of Students | Average Achievement |
| Index based on teachers' responses to two questions about how often they usually assign mathematics homework and how many minutes of mathematics homework they usually assign students (see reference exhibit R3.15). High level indicates the assignment of more than 30 minutes of homework at least once or twice a week. Low level indicates the assignment of less than 30 minutes of homework less than once a week or never assigning homework. Medium level includes all other possible combinations of responses. | Iran, Islamic Rep. <br> Italy <br> Romania <br> Thailand <br> Malaysia | $\begin{array}{ll} 90 & (2.7) \\ 80 & (3.0) \\ 76 & (3.9) \\ 73 & (3.7) \\ 72 & (3.8) \end{array}$ | 421 (3.5) 479 (4.9) 471 (6.7) 473 (6.8) 518 (6.0) | 10 (2.6) <br> 20 (2.9) <br> 24 (3.9) <br> 27 (3.7) <br> 27 (3.8) | $\begin{aligned} & 435(14.9) \\ & 479(7.9) \\ & 477(9.9) \\ & 451(6.9) \\ & 518(9.6) \end{aligned}$ | $\begin{array}{ll} 1 & (0.0) \\ 0 & (0.0) \\ 0 & (0.0) \\ 0 & (0.0) \\ 1 & (0.0) \end{array}$ |  |
|  | Singapore Indonesia <br> Russian Federation <br> Moldova Israel | 66 (4.6) <br> 61 (4.6) <br> 57 (4.6) <br> 57 (4.4) <br> 51 (3.4) | 613 (6.9) <br> 413 (7.3) <br> 527 (6.7) <br> 469 (6.1) <br> 474 (5.4) | 34 (4.6) <br> 39 (4.6) <br> 43 (4.6) <br> 43 (4.4) <br> 49 (3.3) | $\begin{aligned} & 587(10.6) \\ & 394(9.6) \\ & 525(7.8) \\ & 469(6.8) \\ & 459(5.7) \end{aligned}$ | $\begin{array}{ll} 0 & (0.0) \\ 0 & (0.0) \\ 0 & (0.0) \\ 0 & (0.0) \\ 1 & (0.4) \end{array}$ | ~~ |
|  | Turkey <br> Bulgaria <br> Chinese Taipei <br> Hong Kong, SAR <br> Macedonia, Rep. of | 50 (4.0) <br> 49 (5.4) <br> 48 (3.6) <br> 41 (4.3) <br> 39 (4.3) | 437 (5.5) <br> 524 (9.9) <br> 593 (6.4) <br> 580 (5.9) <br> 430 (6.8) | 46 (3.8) <br> 51 (5.4) <br> 50 (3.7) <br> 57 (4.4) <br> 60 (4.3) | $\begin{aligned} & 421(5.4) \\ & 496(7.4) \\ & 580(5.5) \\ & 585(5.8) \\ & 456(5.9) \end{aligned}$ | $\begin{array}{ll} 4 & (1.4) \\ 1 & (0.5) \\ 2 & (1.1) \\ 2 & (1.2) \\ 1 & (0.6) \end{array}$ | $401 \text { (10.2) }$ |
|  | Cyprus Jordan Tunisia England South Africa | 36 (4.4) <br> 32 (3.8) <br> 31 (3.9) <br> 28 (2.9) <br> 25 (3.1) | $\begin{aligned} & 477(3.3) \\ & 423(7.1) \\ & 458(4.6) \\ & 529(8.2) \\ & 261(9.9) \end{aligned}$ | $\begin{array}{ll} 64(4.4) \\ 68 & (3.8) \\ 66 & (4.0) \\ 71 & (3.0) \\ 75 & (3.1) \end{array}$ | 476 (2.6) 428 (5.2) 445 (2.9) 485 (4.7) 281 (7.8) | $\begin{aligned} & 0(0.0) \\ & 0(0.0) \\ & 3(1.5) \\ & 1(0.5) \\ & 0(0.0) \end{aligned}$ | $428 \text { (14.5) }$ |
|  | Lithuania ${ }^{\ddagger}$ <br> United States Korea, Rep. of Latvia (LSS) Chile | $\begin{aligned} & 25(3.7) \\ & 25(2.1) \\ & 25(3.4) \\ & 21(3.5) \\ & 20(3.4) \end{aligned}$ | 504 (9.4) <br> 528 (9.6) <br> 587 (4.2) <br> 514 (8.0) <br> 391 (9.4) | $\begin{array}{ll} 75 & (3.7) \\ 75 & (2.0) \\ 62 & (3.6) \\ 78 & (3.7) \\ 61 & (3.8) \end{array}$ | $\begin{aligned} & 474(4.9) \\ & 495(3.8) \\ & 586(2.9) \\ & 504(4.1) \\ & 390(5.1) \end{aligned}$ | $\begin{array}{r} 0(0.0) \\ 1(0.6) \\ 14(2.6) \\ 2(1.3) \\ 19(2.9) \end{array}$ | $\begin{gathered} 593(4.4) \\ \sim \sim \\ 402(10.8) \end{gathered}$ |
|  | Morocco <br> Hungary <br> Slovenia <br> Canada <br> Philippines | 19 (2.7) <br> 17 (3.1) <br> 17 (2.8) <br> 16 (2.3) <br> 14 (3.0) | $\begin{aligned} & 339(6.1) \\ & 535(9.5) \\ & 529(6.4) \\ & 527(6.2) \\ & 358(15.6) \end{aligned}$ | $\begin{array}{ll} 72 & (3.4) \\ 83 & (3.1) \\ 83 & (2.8) \\ 83 & (2.4) \\ 84 & (3.0) \end{array}$ | $\begin{aligned} & 337(2.8) \\ & 531(4.1) \\ & 530(3.1) \\ & 532(2.8) \\ & 340(6.8) \end{aligned}$ | $\begin{array}{r} 10(1.7) \\ 0(0.0) \\ 0(0.0) \\ 1(0.6) \\ 2(1.1) \end{array}$ | $335 \text { (7.6) }$ |
|  | Japan Netherlands Australia Belgium (Flemish) Finland | $\begin{array}{ll} 11 & (2.5) \\ 11 & (2.6) \\ 11 & (2.7) \\ 10 & (2.0) \\ 10 & (2.3) \end{array}$ | $\begin{aligned} & 578 \text { (3.9) } \\ & 555 \text { (14.6) } \\ & 531 \text { (13.5) } \\ & 582 \text { (8.6) } \\ & 521 \text { (10.8) } \end{aligned}$ | $\begin{array}{ll} 55 & (4.3) \\ 88 & (2.6) \\ 87 & (2.8) \\ 73 & (3.6) \\ 90 & (2.3) \end{array}$ | $\begin{aligned} & 580(2.8) \\ & 538(8.0) \\ & 526(5.4) \\ & 557(5.5) \\ & 521(2.8) \end{aligned}$ | $\begin{array}{r} 34(4.3) \\ 1(0.5) \\ 2(1.0) \\ 17(3.2) \\ 0(0.0) \end{array}$ | $\begin{aligned} 574 & (5.3) \\ \sim & \sim \\ \sim & \sim \\ 548 & \sim(15.0) \\ & \sim \end{aligned}$ |
|  | New Zealand Slovak Republic Czech Republic | $\begin{aligned} & 5(1.8) \\ & 3(1.7) \\ & 2(1.2) \end{aligned}$ | $\begin{gathered} 475(13.1) \\ 554 \text { (28.7) } \\ \sim \sim \end{gathered}$ | 92 (2.1) <br> 94 (2.5) <br> 85 (3.8) | $\begin{aligned} & 495(5.4) \\ & 532(3.9) \\ & 520(4.8) \end{aligned}$ | $\begin{array}{r} 2(1.1) \\ 3(1.8) \\ 13(3.6) \end{array}$ | $\begin{aligned} & 566 \text { (14.6) } \\ & 513 \text { (9.9) } \end{aligned}$ |
|  | International Avg. | 35 (0.6) | 491 (1.8) | 62 (0.6) | 485 (1.0) | 4 (0.2) | 484 (4.0) |

[^19]

Exhibit 6.22 Trends in Index of Teachers' Emphasis on Mathematics Homework (EMH)
TIMSS1999
8
Mathematics

|  | High <br> EMH <br> Percent of Students |  |  |  | Medium <br> EMH <br> Percent of Students |  |  |  | Low <br> EMH <br> Percent of Students |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1995 | 1999 | $\begin{gathered} \text { 1995-1999 } \\ \text { Difference } \end{gathered}$ |  | 1995 | 1999 | $\begin{gathered} \text { 1995-1999 } \\ \text { Difference } \end{gathered}$ |  | 1995 | 1999 | 1995-1999 Difference |  |
| Australia | 8 (1.9) | 11 (2.7) | 3 (3.3) | - | 88 (2.5) | 87 (2.8) | -1 (3.8) | - | 5 (1.6) | 2 (1.0) | -2 (1.9) | 。 |
| Belgium (Flemish) | 14 (2.8) | 10 (2.0) | -3 (3.4) | $\bigcirc$ | 72 (4.1) | 73 (3.6) | 1 (5.4) | - | 15 (3.4) | 17 (3.2) | 2 (4.6) | - |
| Canada | 14 (3.2) | 16 (2.3) | 3 (4.0) | - | 84 (3.3) | 83 (2.4) | -1 (4.1) | $\bullet$ | 3 (1.2) | 1 (0.6) | -2 (1.4) | - |
| Cyprus | 41 (5.8) | 36 (4.4) | -5 (7.3) | $\bigcirc$ | 59 (5.8) | 64 (4.4) | 5 (7.3) | $\bigcirc$ | 0 (0.0) | 0 (0.0) | -- |  |
| Czech Republic | 1 (0.6) | 2 (1.2) | 1 (1.4) | - | 86 (4.1) | 85 (3.8) | -1 (5.6) | - | 13 (4.1) | 13 (3.6) | 0 (5.4) | - |
| England | 47 (3.5) | 28 (2.9) | -20 (4.5) | $\nabla$ | 50 (3.4) | 71 (3.0) | 21 (4.5) | $\triangle$ | 3 (1.0) | 1 (0.5) | -2 (1.1) | - |
| Hong Kong, SAR | 28 (4.8) | 41 (4.3) | 14 (6.5) | - | 68 (5.3) | 57 (4.4) | -10 (7.0) | - | 5 (3.0) | 2 (1.2) | -3 (3.2) | - |
| Hungary | 13 (2.8) | 17 (3.1) | 4 (4.1) | - | 86 (2.8) | 83 (3.1) | -3 (4.2) | - | 1 (0.1) | 0 (0.0) | -1 (0.1) | $\nabla$ |
| Iran, Islamic Rep. | 81 (3.5) | 90 (2.7) | 8 (4.4) | - | 18 (3.4) | 10 (2.6) | -8 (4.3) | - | 1 (0.6) | 1 (0.0) | 0 (0.6) | - |
| Israel ${ }^{\dagger}$ | 45 (8.3) | 52 (3.8) | 6 (9.1) | - | 53 (8.4) | 47 (3.8) | -6 (9.2) | $\bigcirc$ | 1 (0.3) | 1 (0.5) | 0 (0.6) | - |
| Italy | 76 (3.6) | 81 (3.5) | 6 (5.0) | - | 23 (3.6) | 18 (3.4) | -5 (5.0) | - | 1 (0.1) | 0 (0.0) | 0 (0.1) | V |
| Japan | 16 (3.4) | 11 (2.5) | -5 (4.2) | - | 57 (4.3) | 55 (4.3) | -2 (6.1) | $\bullet$ | 27 (3.7) | 34 (4.3) | 7 (5.7) | - |
| Korea, Rep. of | 38 (4.7) | 25 (3.4) | -14 (5.8) | $\bigcirc$ | 57 (4.8) | 62 (3.6) | 5 (6.0) | $\bullet$ | 5 (2.0) | 14 (2.6) | 9 (3.3) | - |
| Latvia (LSS) | 8 (2.6) | 21 (3.5) | 12 (4.4) | $\bigcirc$ | 92 (2.6) | 78 (3.7) | -14 (4.5) | $\nabla$ | 0 (0.0) | 2 (1.3) | 2 (1.3) | - |
| Lithuania | 19 (3.1) | 25 (3.7) | 6 (4.8) | - | 81 (3.1) | 75 (3.7) | -6 (4.8) | - | 0 (0.0) | 0 (0.0) | -- |  |
| Netherlands | 5 (2.4) | 11 (2.6) | 6 (3.5) | $\bigcirc$ | 93 (2.7) | 88 (2.6) | -4 (3.8) | - | 2 (1.4) | 1 (0.5) | -1 (1.5) | - |
| New Zealand | 6 (1.9) | 5 (1.8) | 0 (2.6) | $\bigcirc$ | 89 (2.4) | 92 (2.1) | 3 (3.3) | - | 5 (1.8) | 2 (1.1) | -3 (2.1) | - |
| Romania | 85 (2.9) | 76 (3.9) | -9 (4.9) | $\bigcirc$ | 15 (2.9) | 24 (3.9) | 9 (4.9) | - | 0 (0.0) | 0 (0.0) | -- |  |
| Russian Federation | 54 (4.1) | 57 (4.6) | 3 (6.1) | - | 46 (4.1) | 43 (4.6) | -3 (6.1) | - | 0 (0.0) | 0 (0.0) | - - |  |
| Singapore | 69 (4.6) | 66 (4.6) | -3 (6.4) | - | 30 (4.4) | 34 (4.6) | 4 (6.3) | $\bigcirc$ | 1 (0.9) | 0 (0.0) | -1 (0.9) | - |
| Slovak Republic | 4 (1.7) | 3 (1.7) | -1 (2.4) | - | 95 (1.9) | 94 (2.5) | -1 (3.1) | - | 1 (0.0) | 3 (1.8) | 2 (1.8) | - |
| Slovenia | 22 (3.9) | 17 (2.8) | -5 (4.8) | $\bigcirc$ | 78 (3.9) | 83 (2.8) | 5 (4.8) | $\bullet$ | 0 (0.0) | 0 (0.0) | - - | - |
| Thailand ${ }^{\dagger}$ | 55 (4.9) | 73 (3.7) | 18 (6.1) | $\bigcirc$ | 45 (4.9) | 27 (3.7) | -18 (6.1) | - | 0 (0.0) | 0 (0.0) | -- | - |
| United States | 18 (2.4) | 25 (2.1) | 6 (3.1) | - | 79 (2.4) | 75 (2.0) | -5 (3.2) | - | 3 (0.9) | 1 (0.6) | -2 (1.1) | - |
| International Avg. § | 30 (0.7) | 31 (0.7) | 0 (1.0) | - | 66 (0.8) | 65 (0.7) | -1 (1.1) | - | 4 (0.4) | 4 (0.3) | 0 (0.5) | - |



Background data provided by teachers.
$\dagger$ Countries with unapproved sampling procedures at the classroom level in 1995.
§ International average is for countries that participated and met sampling guidelines in both 1995 and 1999.

Trend notes: Because coverage fell below 65\% in 1995 and 1999, Latvia is annotated LSS for LatvianSpeaking Schools only. Lithuania tested later in 1999 than in 1995, at the beginning of the next school year. In 1995, Italy and Israel were unable to cover their International Desired Population; 1999 data are based on their comparable populations.

Background data for Bulgaria and South Africa are unavailable for 1995.
( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
A dash (-) indicates data are not available.
An " $r$ " indicates teacher response data available for $70-84 \%$ of students, based on the lower response rate in either 1995 or 1999.
$\square$


|  | Percentage of Students by Type of Assessment |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | External Standardized Tests | Teacher-Made Tests Requiring Explanations | Teacher-Made Objective Tests | Homework Assignments | Projects or Practical Exercises | Observations of Students | Students' <br> Responses in Class |
| Australia Belgium (Flemish) Bulgaria Canada Chile | $\begin{array}{ll} 14(3.0) \\ 12 & (3.0) \\ 34 & (4.7) \\ 21 & (3.1) \\ 29 & (3.5) \end{array}$ | 37 (4.5) <br> 94 (1.4) <br> 83 (2.8) <br> 61 (3.0) <br> 79 (3.3) |  $32(4.0)$ <br>  $11(2.4)$ <br>  $31(5.6)$ <br> r $26(2.8)$ <br>  $62(3.6)$ |  $38(3.7)$ <br>  $23(3.0)$ <br>  $81(3.3)$ <br> $r$ $51(3.8)$ <br>  $55(4.0)$ |  $32(3.3)$ <br>  $12(2.1)$ <br>  $30(4.0)$ <br> $r$ $38(2.7)$ <br>  $45(3.9)$ |  | 40 (3.5) <br> 52 (4.4) <br> 99 (0.8) <br> 42 (3.4) <br> 87 (2.2) |
| Chinese Taipei Cyprus Czech Republic England Finland |  $36(4.0)$ <br>  $39(4.7)$ <br>  <br>  <br>  <br>  <br> 5$\quad 53(5.4)$ <br> $51(4.1)$  <br>  $21(3.8)$ | $r$$43(4.0)$ <br> $59(4.8)$ <br>  <br>  <br> 5 <br> $97(1.8)$ <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br> $18(3.6)$ | $\begin{array}{rr}  & 76(3.4) \\ \text { r } & 37(4.7) \\ & 9(2.6) \\ \text { s } & 7(1.4) \\ & 20(3.3) \end{array}$ |  | $r$$17(3.4)$ <br> $66(4.0)$ <br>  <br>  <br> 5$23(5.2)$ <br>  <br> $41(3.4)$ <br>  <br>  <br>  <br> $52(4.1)$ | $\begin{array}{ll}  & 68(3.1) \\ \mathrm{r} & 99(0.9) \\ & 80(4.2) \\ \mathrm{s} & 78(2.9) \\ & 83(3.6) \end{array}$ | $\begin{array}{ll}  & 72(3.6) \\ \mathrm{r} & 99(1.0) \\ & 98(1.5) \\ \mathrm{s} & 78(2.7) \\ & 90(2.9) \end{array}$ |
| Hong Kong, SAR <br> Hungary <br> Indonesia <br> Iran, Islamic Rep. <br> Israel | $\begin{array}{ll} 17 & (3.2) \\ 44 & (4.1) \\ 50 & (4.8) \\ 76 & (3.8) \\ 10 & (2.0) \end{array}$ | $\begin{array}{ll} 52(4.2) \\ 66 & (4.1) \\ 81 & (3.2) \\ 79 & (3.4) \\ 78 & (3.3) \end{array}$ | $\begin{aligned} & 47(3.6) \\ & 17(3.1) \\ & 44(4.8) \\ & 46(4.3) \\ & 28(3.5) \end{aligned}$ | 44 (4.0) <br> 36 (3.9) <br> 65 (4.3) <br> 78 (3.2) <br> 53 (3.5) | $\begin{aligned} & 10(2.6) \\ & 62(3.8) \\ & 72(4.3) \\ & 20(2.8) \\ & 40(3.9) \end{aligned}$ | $\begin{array}{ll} 38 & (4.3) \\ 71 & (3.7) \\ 76 & (4.1) \\ 38 & (4.0) \\ 44 & (3.2) \end{array}$ | 44 (4.3) <br> 88 (2.9) <br> 81 (3.7) <br> 86 (3.1) <br> 59 (3.3) |
| Italy <br> Japan <br> Jordan <br> Korea, Rep. of Latvia (LSS) | $\begin{array}{ll} 22 & (3.2) \\ 15 & (2.9) \\ 30 & (4.0) \\ 37 & (3.8) \\ 80 & (3.8) \end{array}$ | $\begin{array}{ll} 92 & (2.2) \\ 55 & (4.4) \\ 78 & (3.8) \\ 48 & (3.7) \\ 81 & (4.1) \end{array}$ | $\begin{array}{ll} 63 & (3.8) \\ 25 & (3.9) \\ 32 & (4.2) \\ 45 & (3.7) \\ 50 & (4.6) \end{array}$ | 67 (3.6) <br> 47 (4.0) <br> 70 (3.7) <br> 32 (3.6) <br> 63 (4.6) | $\begin{array}{ll} 75 & (3.1) \\ 41 & (4.0) \\ 41 & (4.3) \\ 43 & (3.3) \\ 69 & (4.3) \end{array}$ | 96 (1.4) <br> 67 (4.1) <br> 82 (3.1) <br> 50 (4.1) <br> 79 (3.7) | 99 (0.6) <br> 65 (4.3) <br> 88 (2.6) <br> 61 (4.1) <br> 98 (1.2) |
| Lithuania ${ }^{\ddagger}$ Macedonia, Rep. of Malaysia Moldova Morocco | 35 (3.9) <br> 69 (4.3) <br> 18 (3.2) <br> 60 (4.6) <br> 30 (2.9) | 57 (4.3) <br> 63 (4.1) <br> 38 (4.1) <br> 95 (2.0) <br> 74 (3.1) | 14 (2.7) <br> 65 (4.2) <br> 66 (4.2) <br> 55 (4.3) <br> 42 (3.0) | 25 (3.4) <br> 85 (3.1) <br> 84 (3.2) <br> 84 (3.5) <br> 80 (2.7) | 18 (3.5) <br> 47 (4.2) <br> 32 (4.2) <br> 48 (4.5) <br> 78 (2.2) | $\begin{array}{ll} 27 & (3.7) \\ 98 & (1.5) \\ 76 & (3.7) \\ 85 & (3.0) \\ 78 & (2.5) \end{array}$ | $\begin{array}{r} 75(3.7) \\ 100(0.0) \\ 86(2.8) \\ 88(2.6) \\ 87(1.8) \end{array}$ |
| > Netherlands > New Zealand Philippines Romania Russian Federation | $\begin{gathered} 29(5.5) \\ 16(3.0) \\ 38(4.1) \\ 66(4.0) \\ -- \end{gathered}$ | $\begin{aligned} & 96(1.8) \\ & 59(4.2) \\ & 74(4.0) \\ & 80(3.4) \\ & 98(1.0) \end{aligned}$ | $\begin{array}{ll} 20 & (5.8) \\ 23 & (3.5) \\ 73 & (4.0) \\ 55 & (4.2) \\ 54 & (4.4) \end{array}$ | $\begin{array}{ll} 18(4.7) \\ 39 & (4.0) \\ 79 & (3.4) \\ 79 & (3.2) \\ 68 & (3.7) \end{array}$ | $\begin{array}{r} 8(2.6) \\ 29(3.6) \\ 72(4.4) \\ 35(4.3) \\ 59(3.8) \end{array}$ | $\begin{array}{ll} 28 & (4.7) \\ 55 & (4.5) \\ 77 & (3.4) \\ 86 & (2.6) \\ 91 & (2.2) \end{array}$ | $\begin{array}{ll} 27 & (5.4) \\ 55 & (4.6) \\ 95 & (1.9) \\ 98 & (1.2) \\ 86 & (2.5) \end{array}$ |
| Singapore Slovak Republic Slovenia South Africa Thailand | $\begin{array}{ll} 36 & (4.2) \\ 79 & (4.2) \\ 41 & (4.8) \\ 39 & (4.3) \\ 28 & (4.0) \end{array}$ | $\begin{aligned} & 22(3.9) \\ & 89(3.1) \\ & 61(3.9) \\ & 55(4.1) \\ & 70(3.6) \end{aligned}$ | $\begin{array}{r} 5(2.0) \\ 56(5.5) \\ 14(2.7) \\ 49(4.7) \\ 72(3.7) \end{array}$ | 61 (4.5) <br> 29 (4.3) <br> 51 (4.3) <br> 74 (4.4) <br> 80 (3.5) | 37 (4.2) <br> 69 (4.9) <br> 32 (3.8) <br> 35 (4.1) <br> 43 (4.0) | 46 (4.6) <br> 83 (3.1) <br> 46 (4.2) <br> 58 (3.4) <br> 60 (3.9) | $\begin{array}{ll} 52 & (4.2) \\ 98 & (1.1) \\ 82 & (3.4) \\ 76 & (3.4) \\ 71 & (3.7) \end{array}$ |
| Tunisia <br> Turkey <br> United States | $\begin{array}{ll} 24 & (3.7) \\ 24 & (3.1) \\ 28 & (3.0) \end{array}$ | $\begin{aligned} & 78 \\ & 78 \\ & 50 \\ & 50 \end{aligned}(4.3)$ | $\begin{array}{ll} 64 & (4.1) \\ 35 & (4.4) \\ 28 & (3.5) \end{array}$ | $\begin{array}{ll} 76 & (3.8) \\ 58 & (3.4) \\ 56 & (4.3) \end{array}$ | $\begin{array}{ll} 62 & (4.1) \\ 31 & (3.7) \\ 33 & (3.5) \end{array}$ | $\begin{array}{ll} 74 & (4.0) \\ 51 & (4.3) \\ 40 & (3.2) \end{array}$ | $\begin{array}{ll} 89 & (2.8) \\ 96 & (1.5) \\ 41 & (3.6) \end{array}$ |
| International Avg. | 37 (0.6) | 67 (0.6) | 39 (0.6) | 60 (0.6) | 42 (0.6) | 64 (0.6) | 77 (0.5) |

[^20][^21]


[^0]:    Background data provided by teachers.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^1]:    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
    An " $r$ " indicates teacher response data available for $70-84 \%$ of students. An " $s$ " indicates teacher response data available for $50-69 \%$ of students.

[^2]:    Background data provided by teachers.
    1 Teachers having mathematics as the major area of study are those who reported having a bachelor's degree (BA) or equivalent, master's degree (MA), or teacher training certificate in mathematics or mathematics education.
    2 Includes teachers certified to teach any subject.
    3 Italy: Teacher training certificate not required but teachers must excel on a national exam.

[^3]:    1 Beaton, A.E., Mullis, I.V.S., Martin, M.O., Gonzalez, E.J., Kelly, D.L., and Smith, T.A. (1996), Mathematics Achievement in the Middle School Years: IEA's Third International Mathematics and Science Study, Chestnut Hill MA: Boston College.

[^4]:    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.

[^5]:    2 Stigler, J.W., Gonzales, P., Kawanaka, T., Knoll, S., and Serrano, A., (1999), The TIMSS Videotape Classroom Study: Methods and Findings from an Exploratory Research Project on Eighth-Grade Mathematics Instruction in Germany, Japan, and the United States, NCES 1999-074, Washington DC: National Center for Education Statistics.

[^6]:    Mathematics instructional time provided by teachers, and total instructional time provided by schools.
    1 Computed as the ratio of mathematics instructional time to total instructional time averaged across students.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning at the next school year.

[^7]:    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates data are not available.
    An " $r$ " indicates school and/or teacher response data available for $70-84 \%$ of students. An " $s$ " indicates school and/or teacher response data available for $50-69 \%$ of students. An "x" indicates school and/or teacher response data available for $<50 \%$ of students.

[^8]:    A dash (-) indicates data are not available. A tilde (~) indicates insufficient data to report achievement.
    An " $r$ " indicates teacher response data available for 70-84\% of students. An "s" indicates teacher response data available for 50-69\% of students.

[^9]:    Background data provided by students.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^10]:    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number some totals may appear inconsistent.
    A dash ( - ) indicates data are not available. A tilde ( ) indicates insufficient data to report achievement.
    An " $r$ " indicates a $70-84 \%$ student response rate.

[^11]:    Background data provided by teachers.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A tilde ( $\sim$ ) indicates insufficient data to report achievement.

[^12]:    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^13]:    A tilde ( ) indicates insufficient data to report achievement.
    An " $r$ " indicates teacher response data available for 70-84\% of students. An "s" indicates teacher response data available for 50-69\% of students.

[^14]:    Background data provided by teachers.

    * The use of calculators on TIMSS was not allowed in 1995 or in 1999
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

[^15]:    A dash (-) indicates data are not available. A tilde (~) indicates insufficient data to report achievement.
    An "r" indicates teacher and/or student response data available for $70-84 \%$ of students. An "s" indicates teacher and/or student response data available for 50-69\% of students.

[^16]:    Background data provided by students.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^17]:    Background data provided by students.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.

    A dash (-) indicates data are not available.
    $A n$ " $r$ " indicates a $70-84 \%$ student response rate. An " $s$ " indicates a $50-69 \%$ student response rate.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^18]:    3 Robitaille, D.F., (1997), National Contexts for Mathematics and Science Education: An Encyclopedia of the Education Systems Participating in TIMSS, Vancouver, BC: Pacific Educational Press.

[^19]:    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    () Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent

[^20]:    Background data provided by teachers.
    $\ddagger$ Lithuania tested the same cohort of students as other countries, but later in 1999, at the beginning of the next school year.
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.

[^21]:    A dash (-) indicates data are not available.
    An " r " indicates teacher response data available for $70-84 \%$ of students. An " s " indicates teacher response data available for $50-69 \%$ of students.

